

Thermoelectric Silicon: From Fundamental Physics to Real-World Applications

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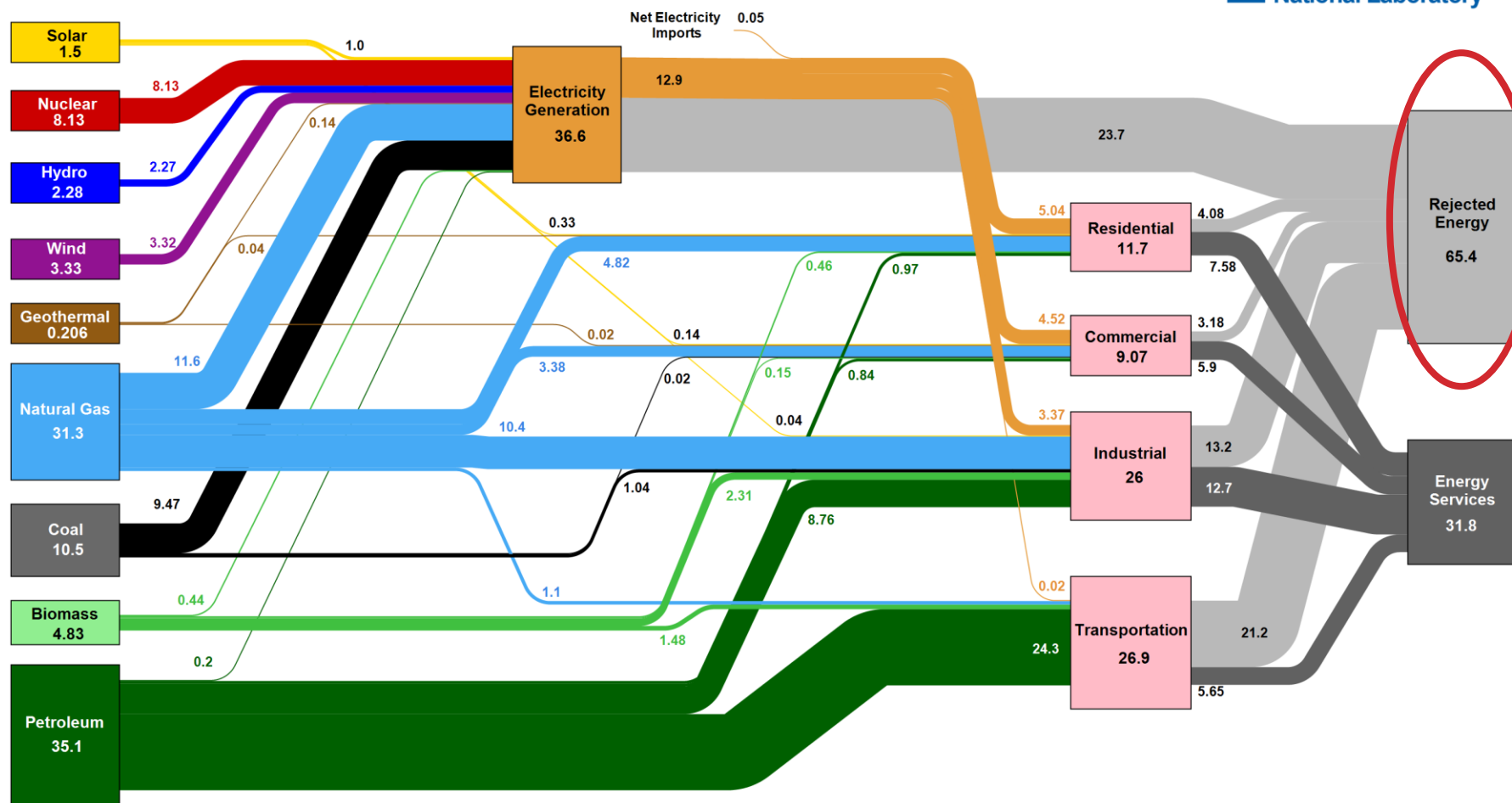


- Why Heat Harvesting Matters
- Thermoelectricity: Physics and Technology
- Materials Issues
- Silicon as a New Player for Thermoelectrics:
 - SiGe alloys for RTGs
 - Si at low temperatures: Nanowires
 - Si at low temperatures: Thin Films
- From Materials to Devices
- Applications
- Some Conclusions

Why Heat Harvesting Matters

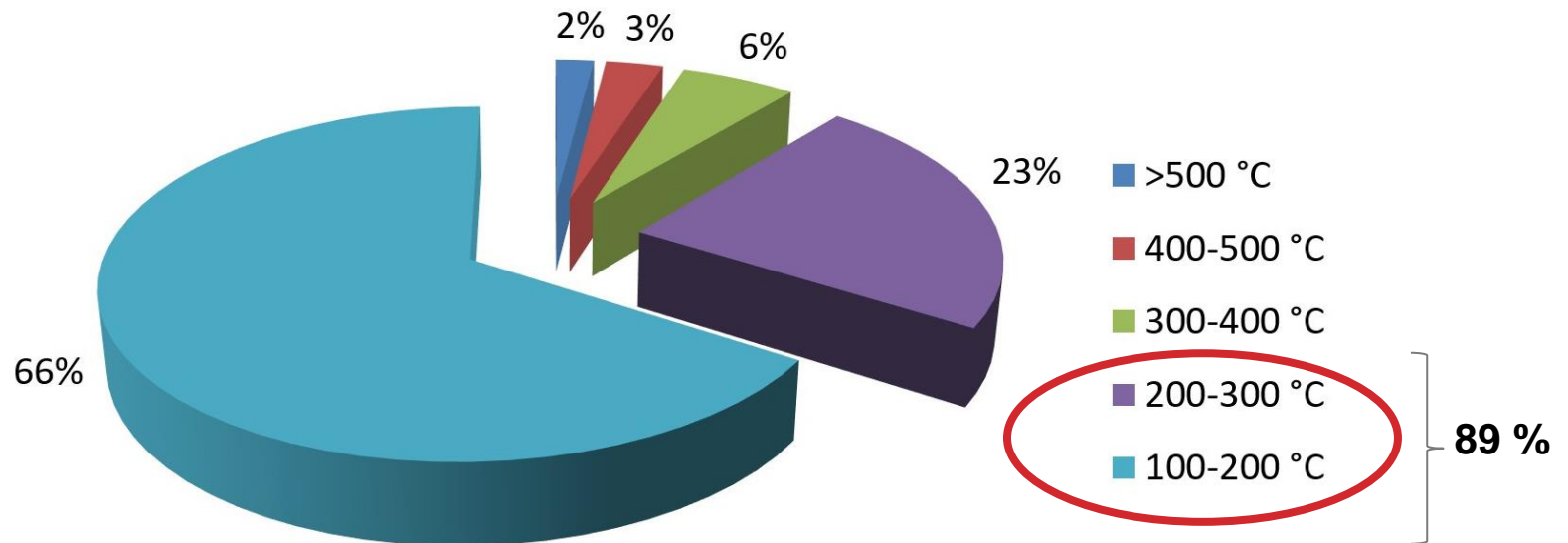
Estimated U.S. Energy Consumption in 2021: 97.3 Quads

Lawrence Livermore
National Laboratory



Source: LLNL March, 2022. Data is based on DOE/EIA MER (2021). If this information or a reproduction of it is used, credit must be given to the Lawrence Livermore National Laboratory and the Department of Energy, under whose auspices the work was performed. Distributed electricity represents only retail electricity sales and does not include self-generation. EIA reports consumption of renewable resources (i.e., hydro, wind, geothermal and solar) for electricity in BTU-equivalent values by assuming a typical fossil fuel plant heat rate. The efficiency of electricity production is calculated as the total retail electricity delivered divided by the primary energy input into electricity generation. End use efficiency is estimated as 65% for the residential sector, 65% for the commercial sector, 21% for the transportation sector and 49% for the industrial sector, which was updated in 2017 to reflect DOE's analysis of manufacturing. Totals may not equal sum of components due to independent rounding. LLNL-MI-410527

Why Heat Harvesting Matters



Thermoelectricity and Classical Irreversible Thermodynamics

$$\begin{cases} J_q = \kappa T^2 \frac{d(1/T)}{dx} \\ J_e = \sigma T \left(\frac{F}{T} \right) \end{cases}$$

Fourier's law

Ohm's law

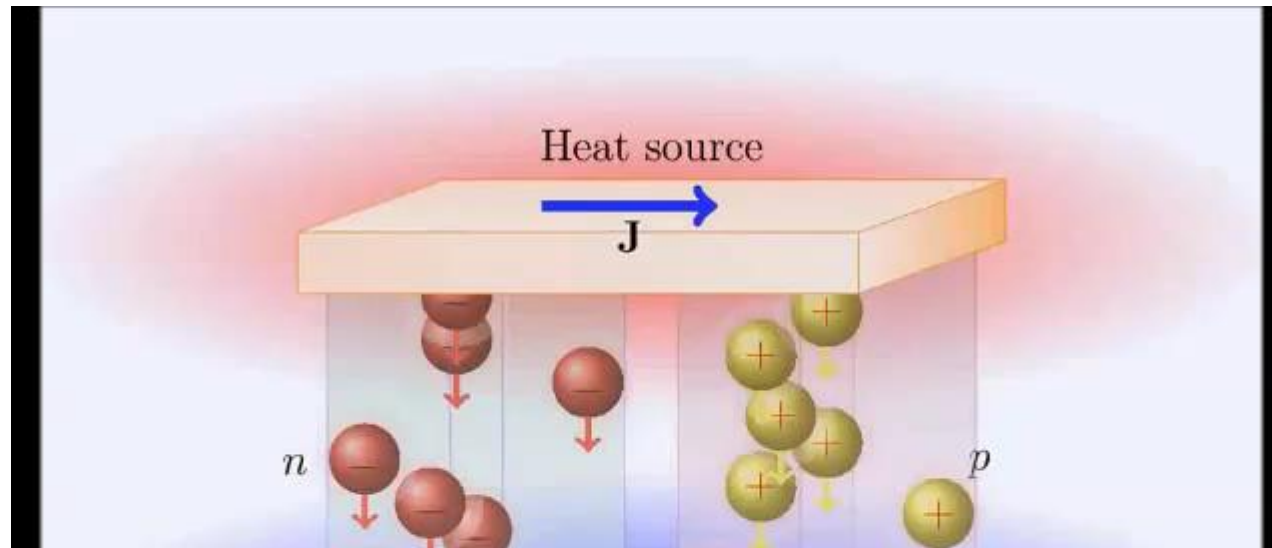
In an open circuit ($J_e = 0$), $-L_{eq} \frac{dT}{dx} + \sigma F T^2 = 0$ so that

$$L_{eq} = \sigma T^2 \left(-\frac{\Delta V}{\Delta T} \right) = \sigma T^2 \alpha$$

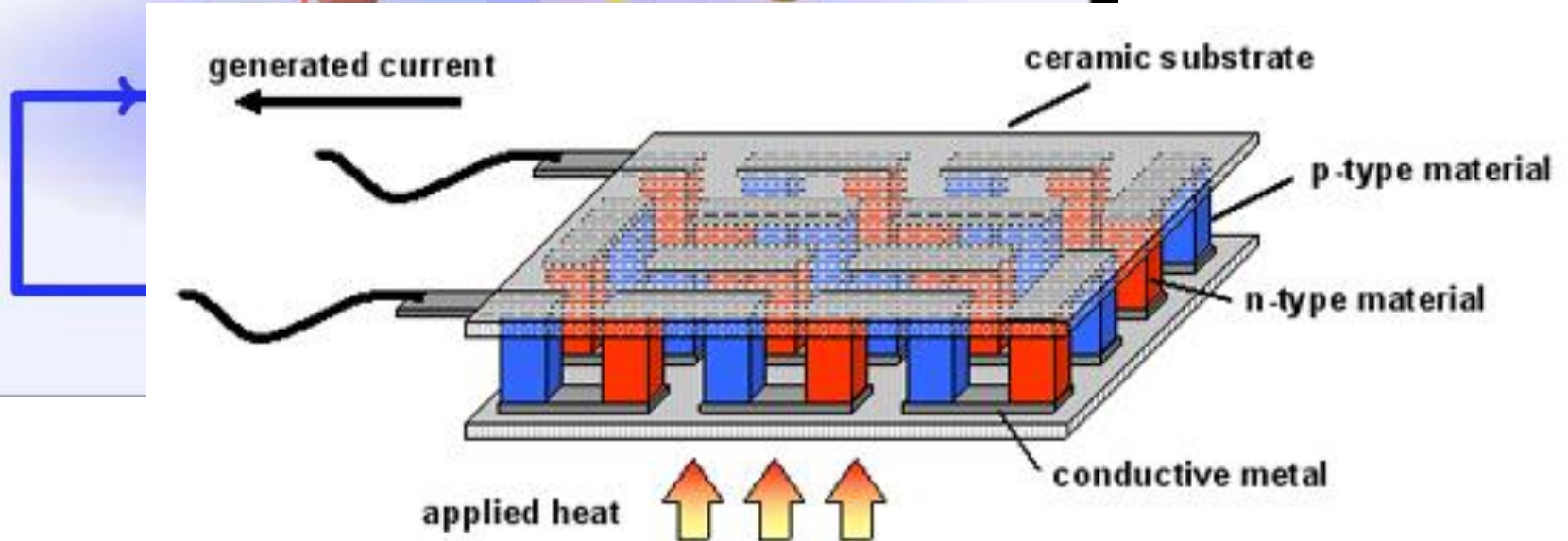
In a short circuit and for $\frac{dT}{dx} = 0$ we get $J_q / J_e = L_{qe} / (\sigma T)$ whence

$$\Pi \equiv J_q / J_e = \sigma T^2 \alpha \times \frac{1}{\sigma T} = \alpha T$$

Thermoelectricity: the basics

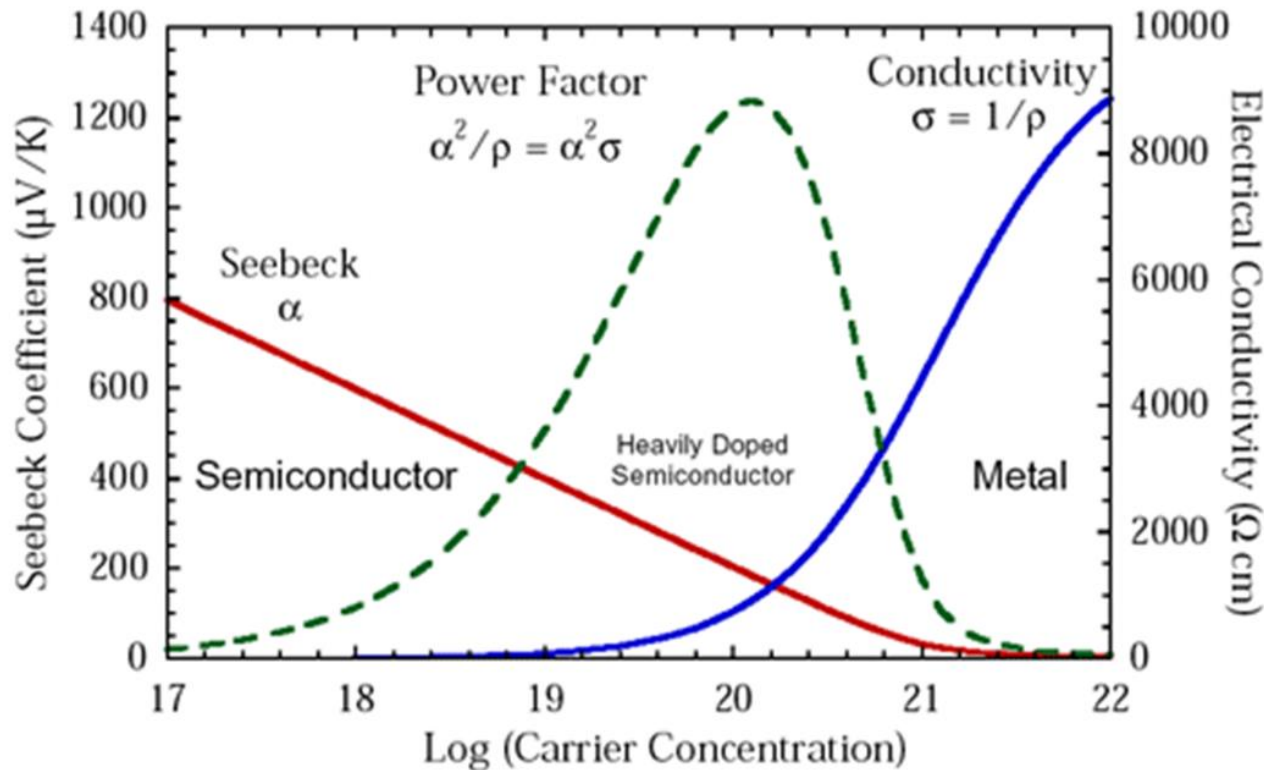


$$ZT = \frac{\sigma \alpha^2}{\kappa} T$$



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Good thermoelectrics require 'miracle materials', with large electrical conductivity, a low thermal conductivity, and a high Seebeck coefficient



$$ZT = \frac{\sigma \alpha^2}{\kappa} T$$

The Materials Challenge

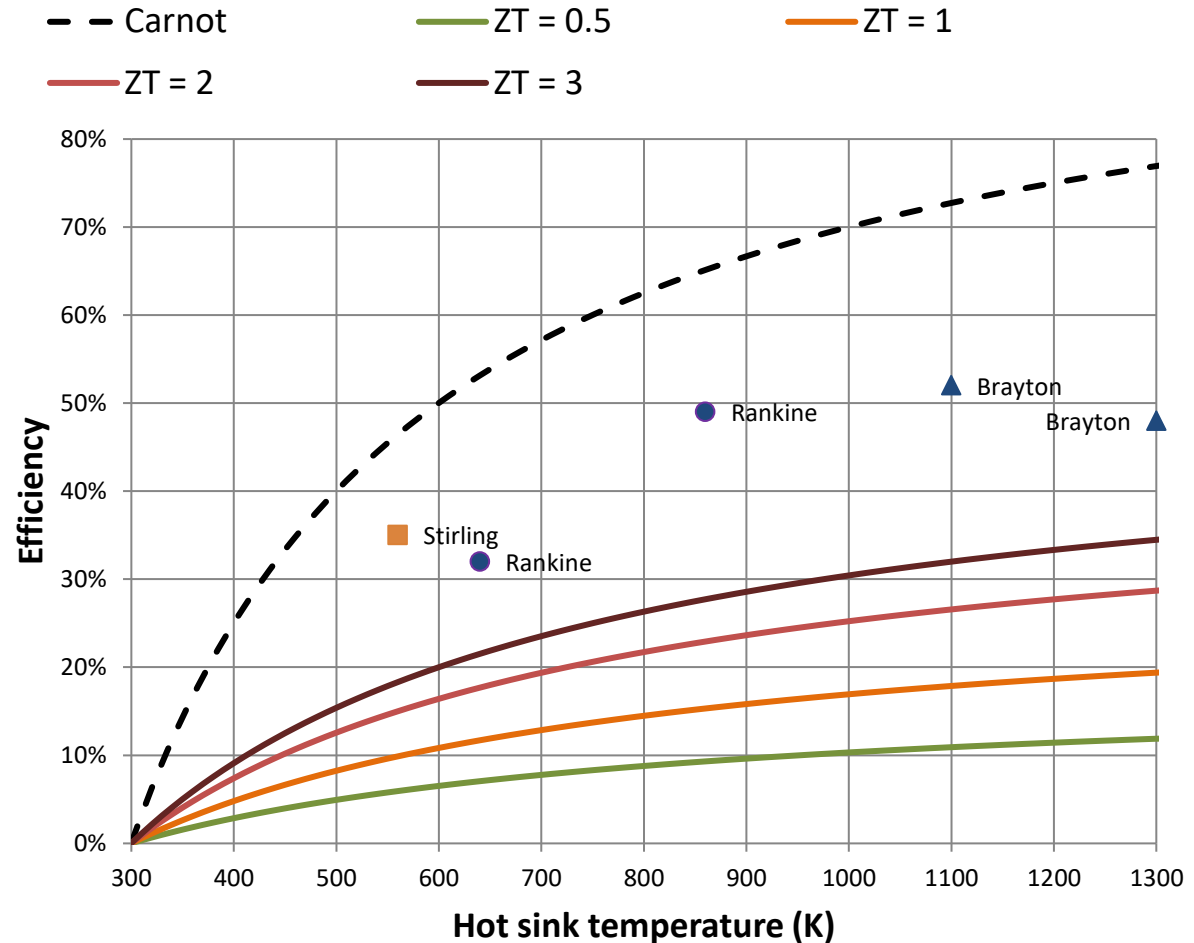
Thermoelectrics must overcome the competition of standard heat engines but also of other energy harvesting devices

Pro's

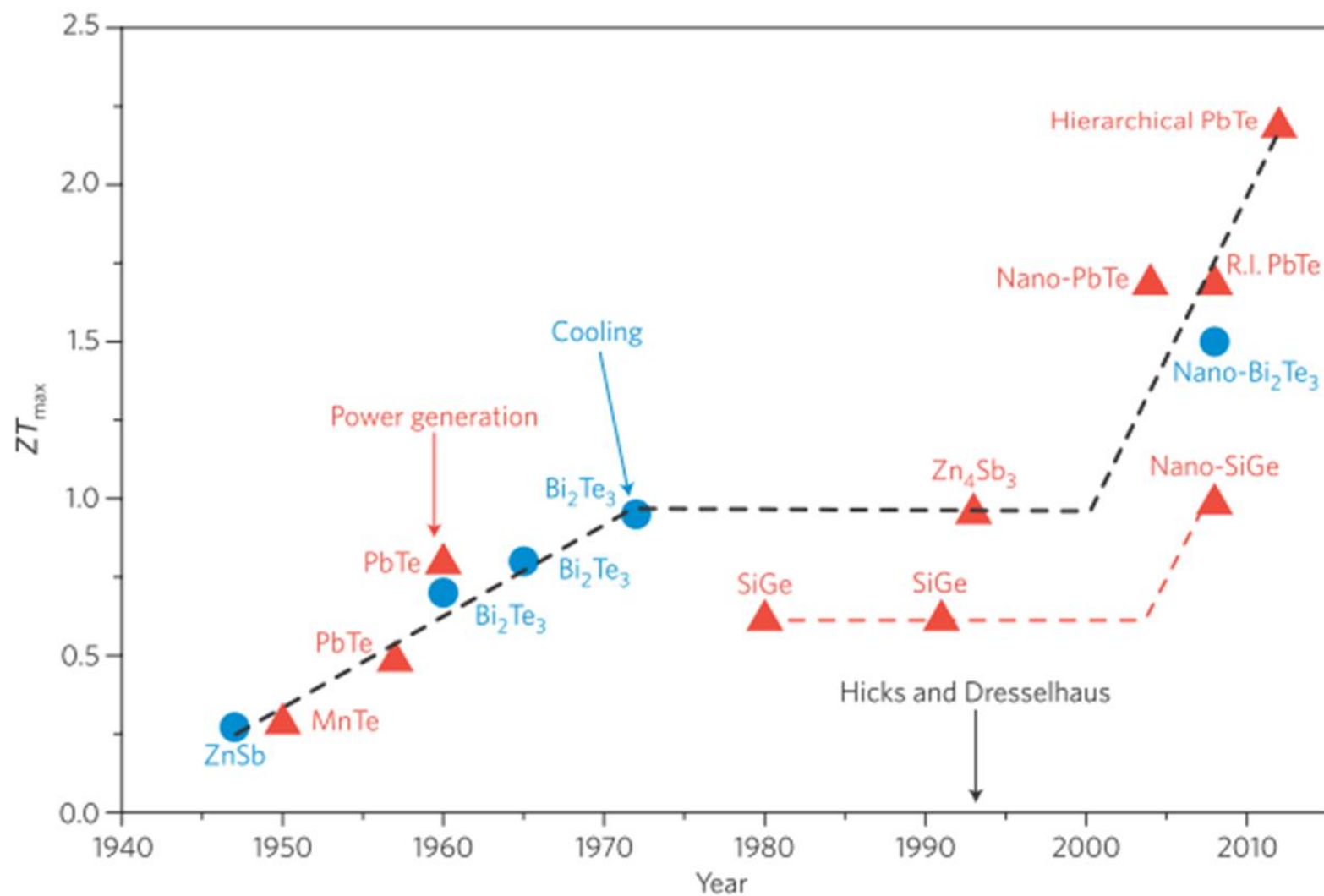
- No moving parts
- High reliability & lifetime
- Can be miniaturized
- Efficient at low T

Con's

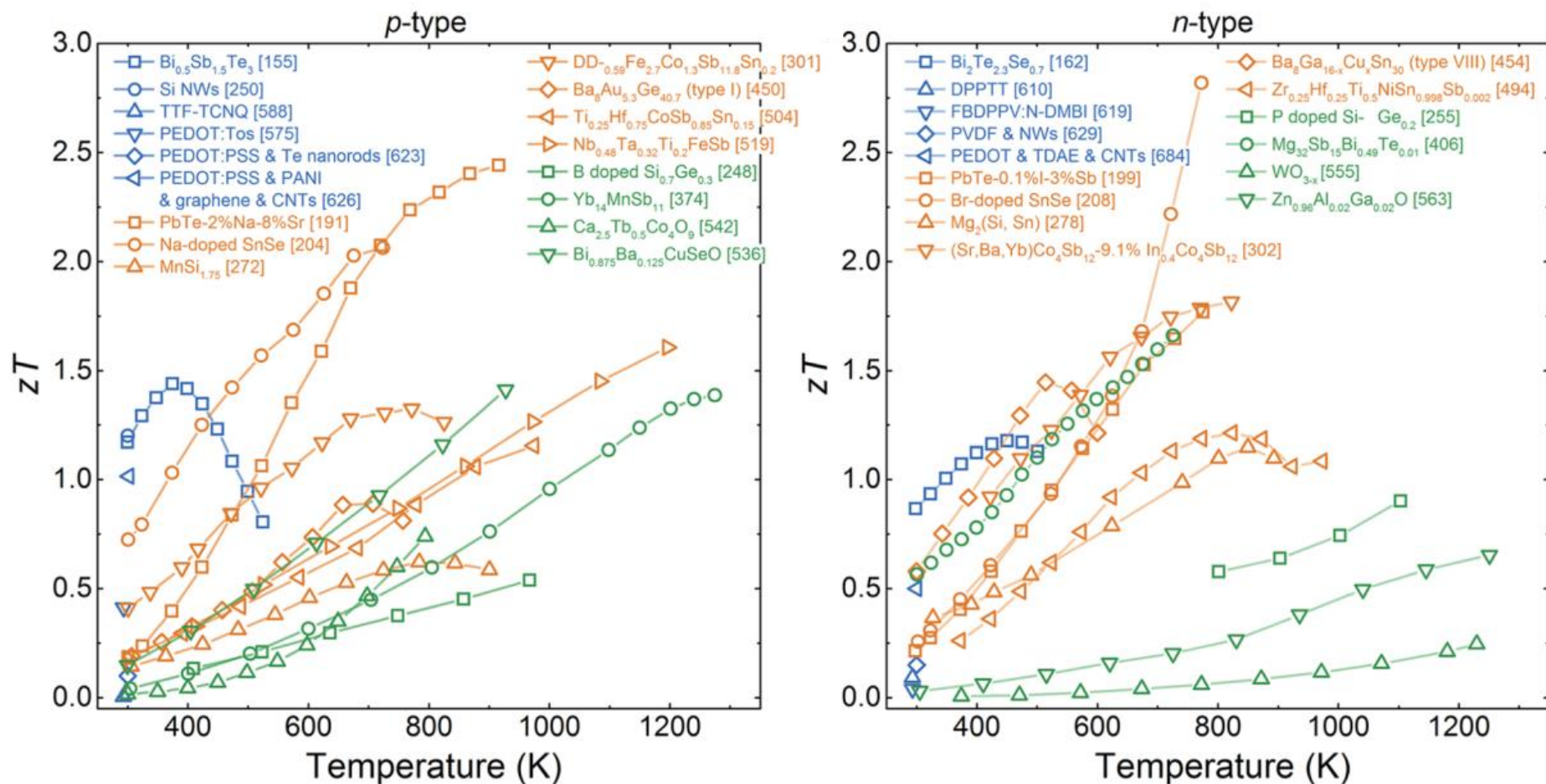
- Low efficiency
- Expensive



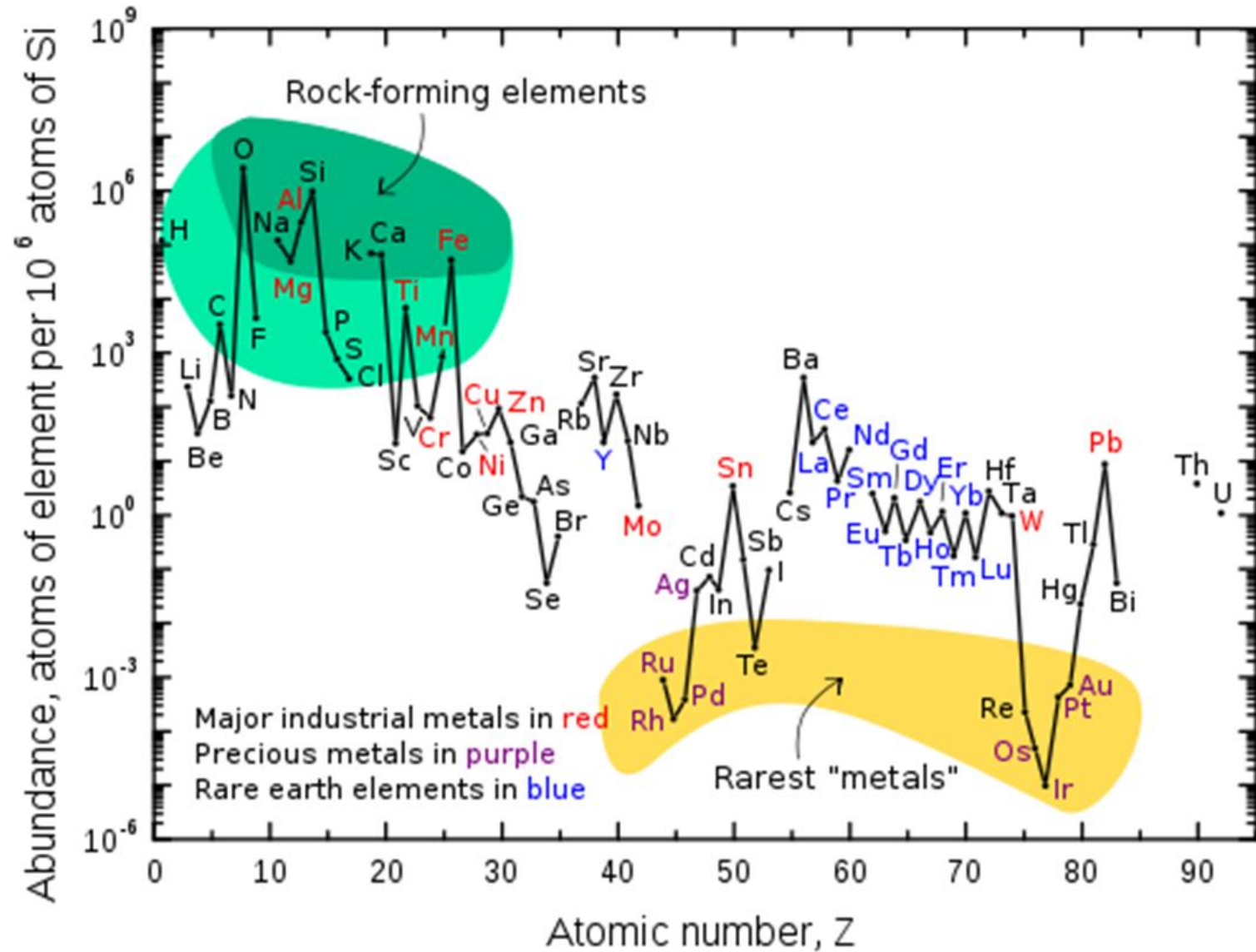
The Materials Challenge



The Materials Challenge



The Materials Challenge



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Silicon as a New Player for Thermoelectrics

Strong need for largely geo-available TE materials operating around room temperature:

- heat body harvesting
- hybrid solar conversion
- cooling and heat management

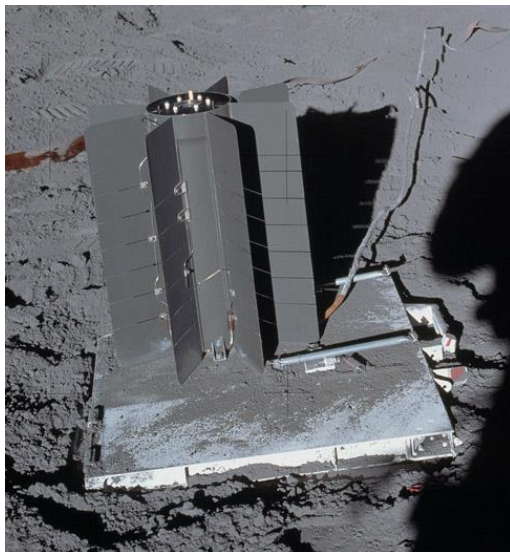
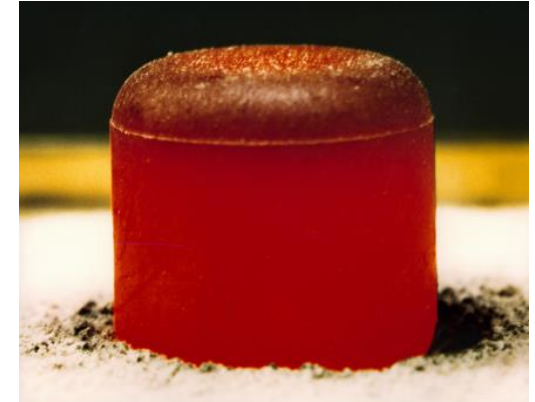
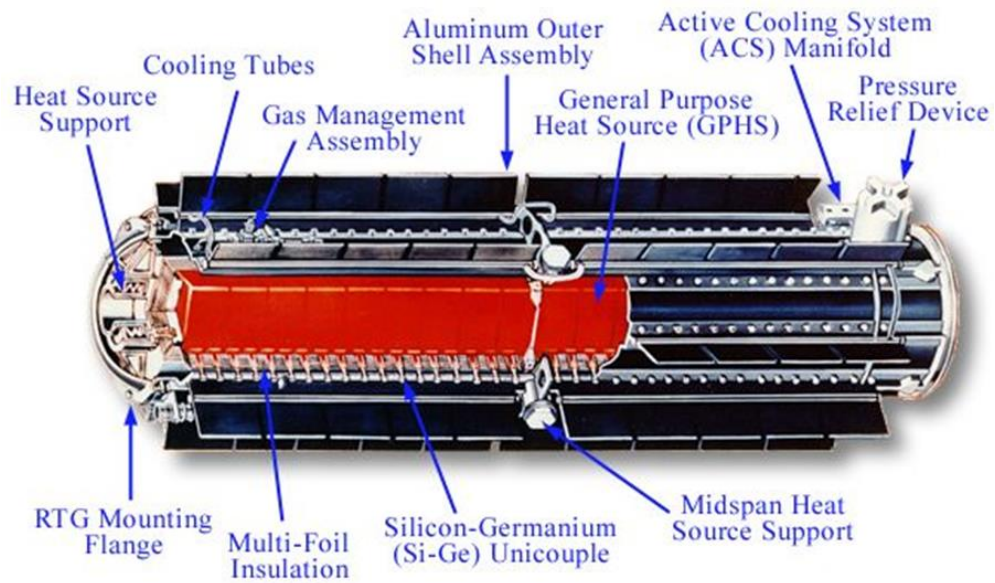
Silicon (as SiGe alloys) seen in the past for high-temp applications. Nanotechnology has shown instead its usability around room temp:

- Si nanowires
- Si nanopillars
- Si thin films

Si nanowires & thin films disclose power factors and ZT fully comparable to tellurides, providing an IC-compatible, mature and geo-abundant competitor

SiGe Alloys and Space Exploration

GPHS-RTG



SNAP-27 on the Moon (Apollo 12)
70 W_e

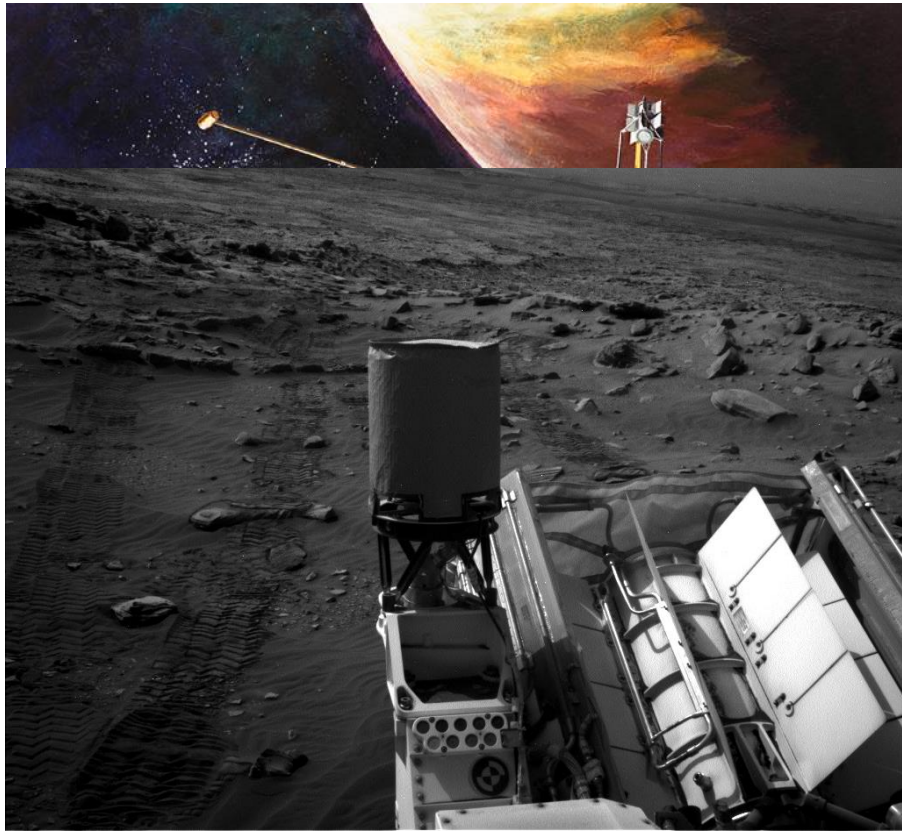
SNAP on Nimbus III (1968)
28.2 W_e



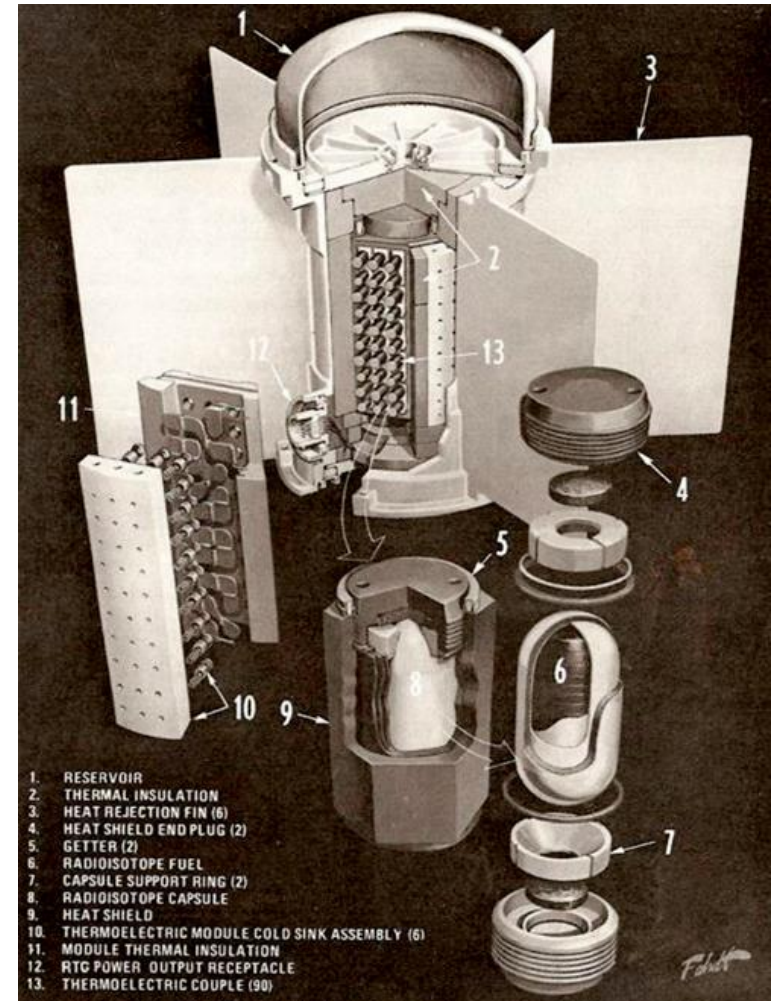
SiGe Alloys and Space Exploration

Pioneer 2 – Launched in 1972

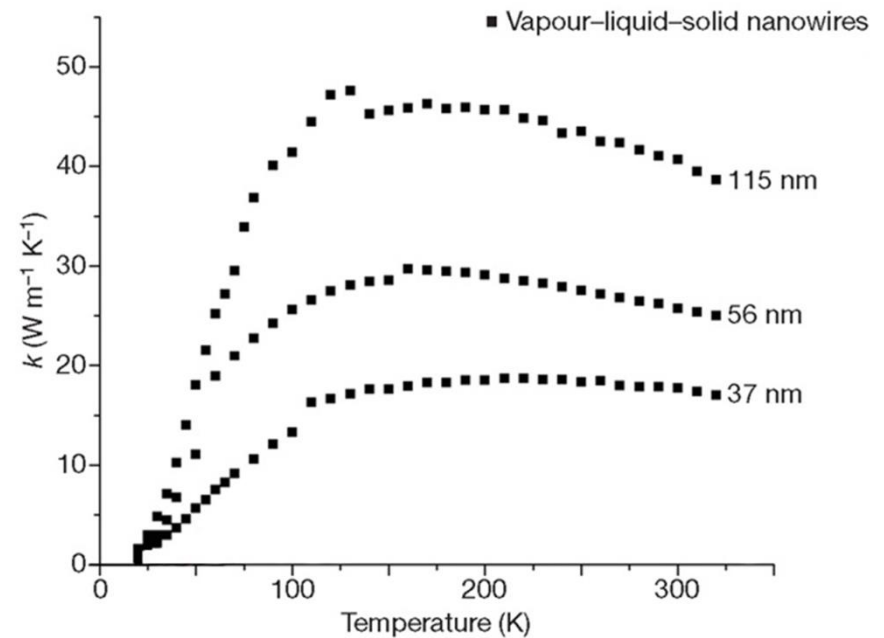
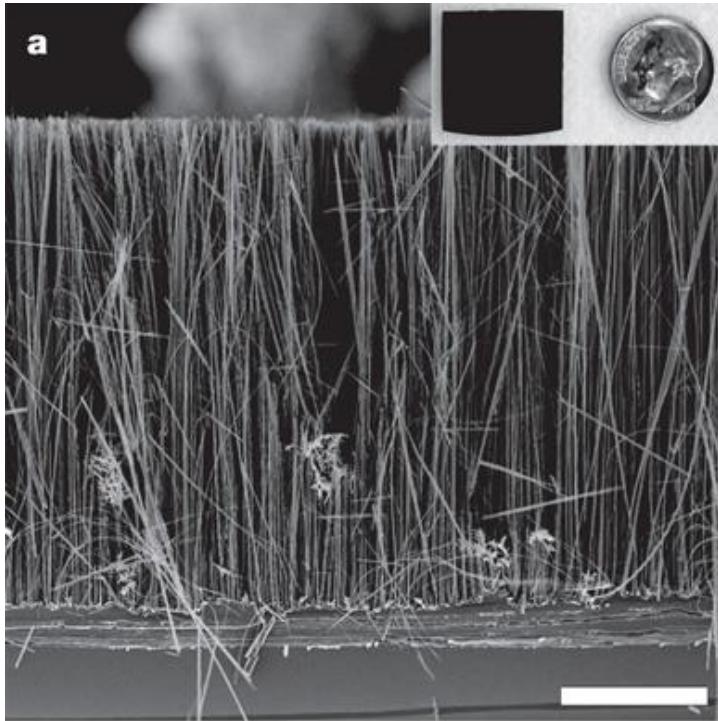
RTEG still working in 2002 when leaving the solar system



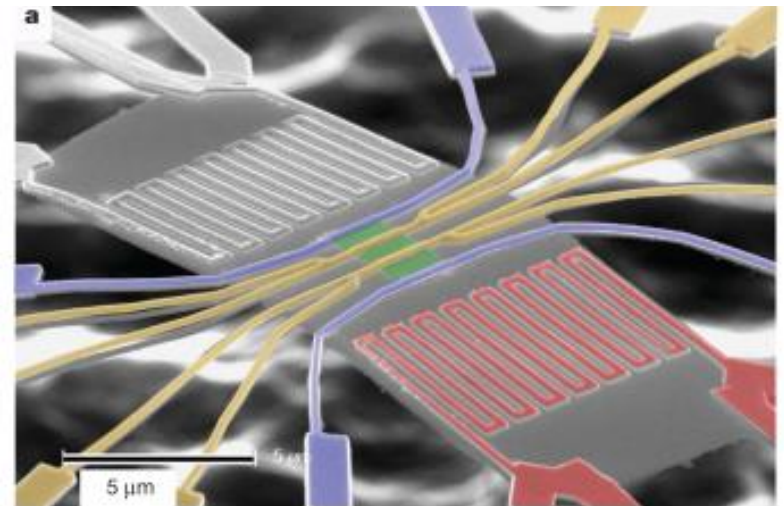
GPHS-RTG powering Curiosity
292 W_e



Silicon at Low Temperatures: Nanowires

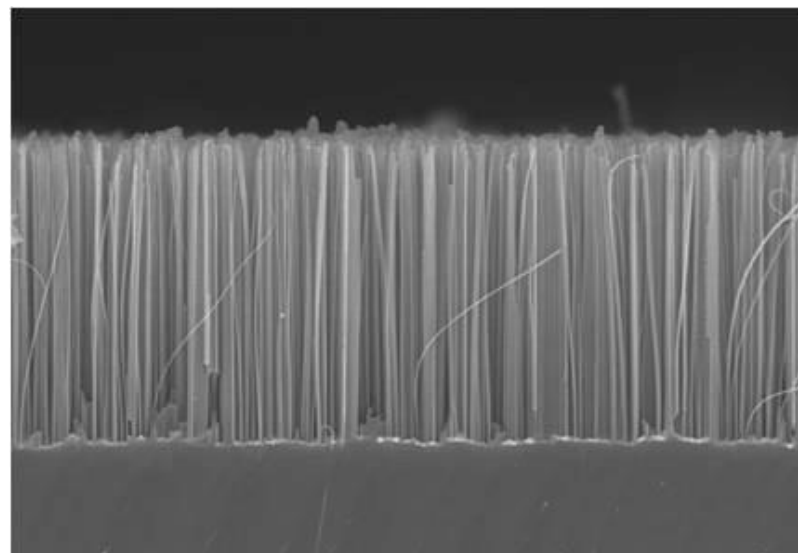
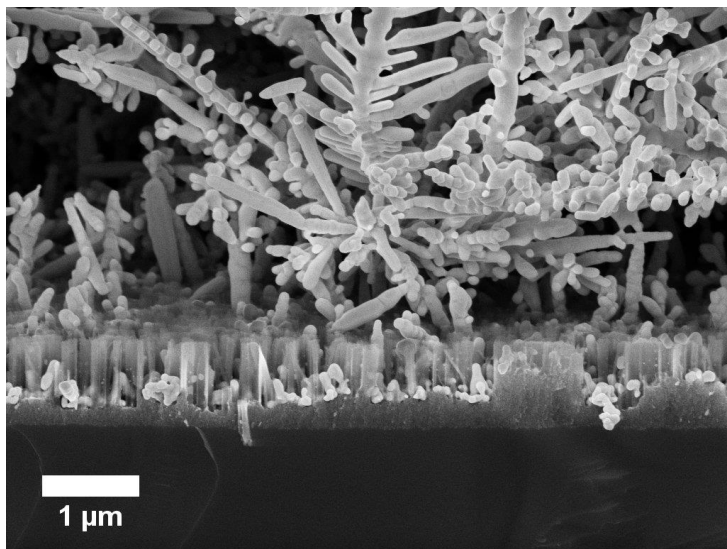
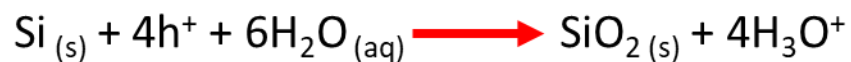


Incoherent phonon scattering along with coherent electron scattering at NW walls let σ/k increase by two orders of magnitude

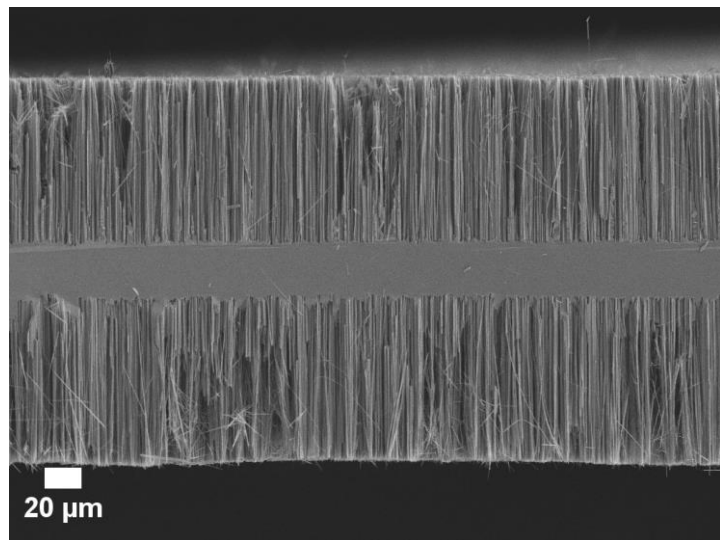


A.I. Boukai et al., Nature 451(7175), 168–171 (2008)
 A.I. Hochbaum et al., Nature 451(7175), 163–167 (2008)

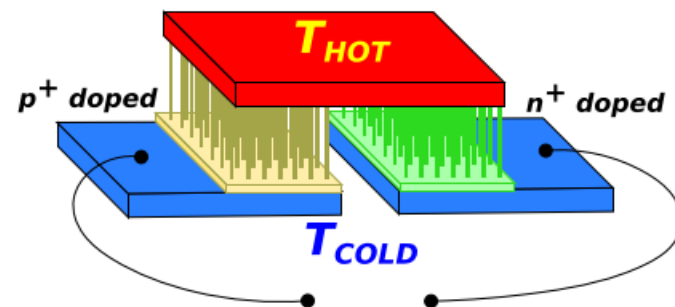
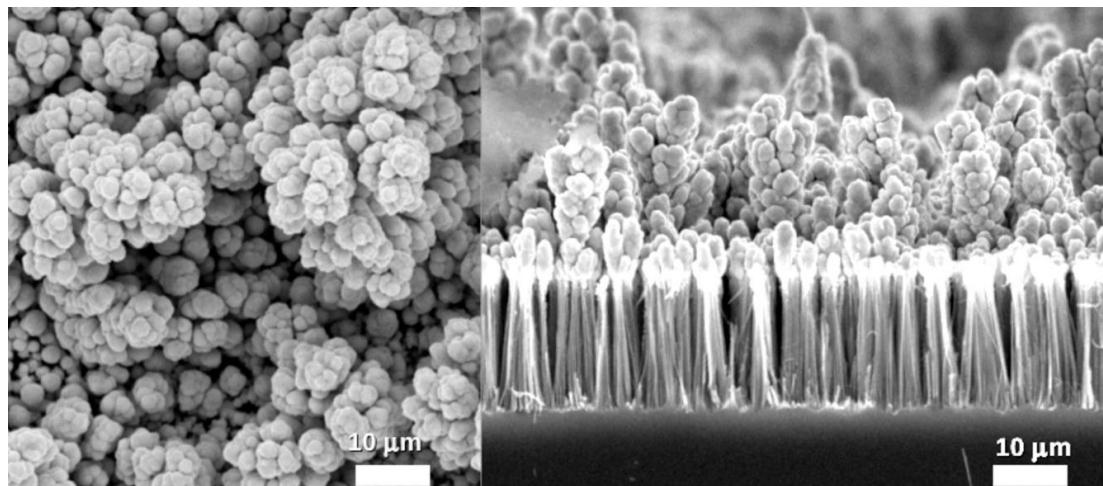
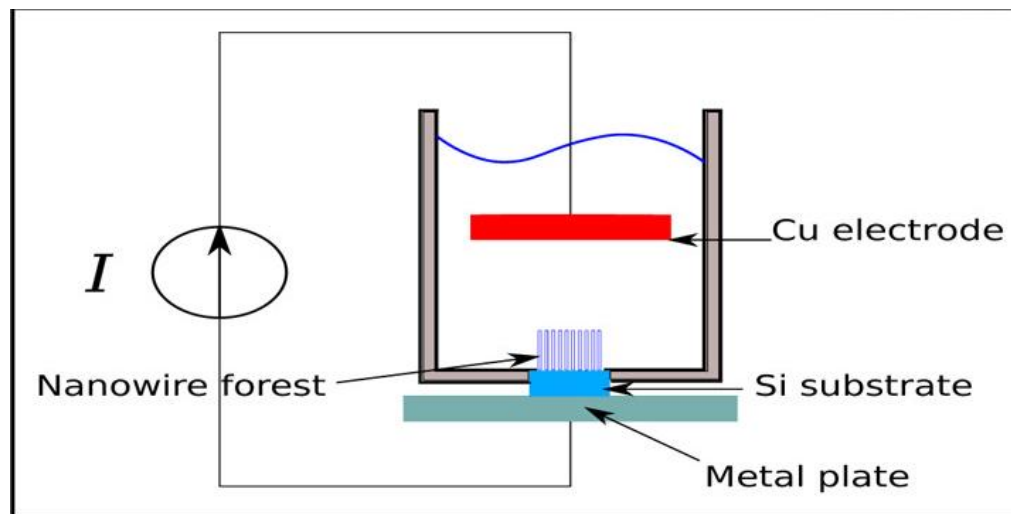
Metal-Assisted Chemical Etching (MACE)



Silicon at Low Temperatures: Nanowires



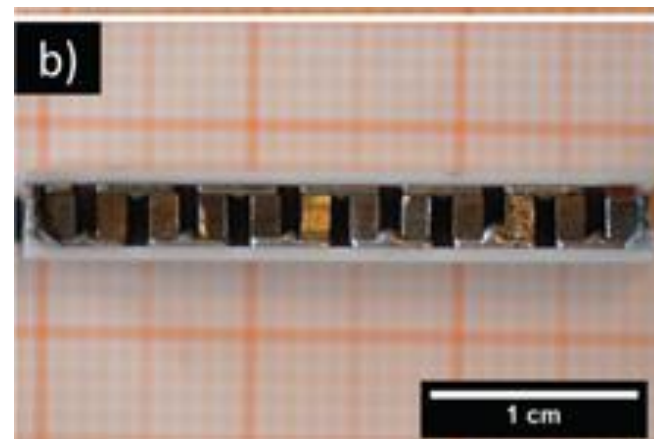
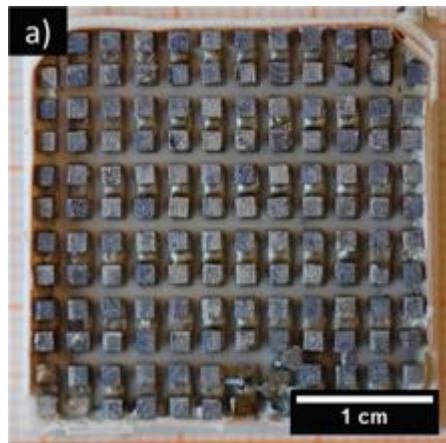
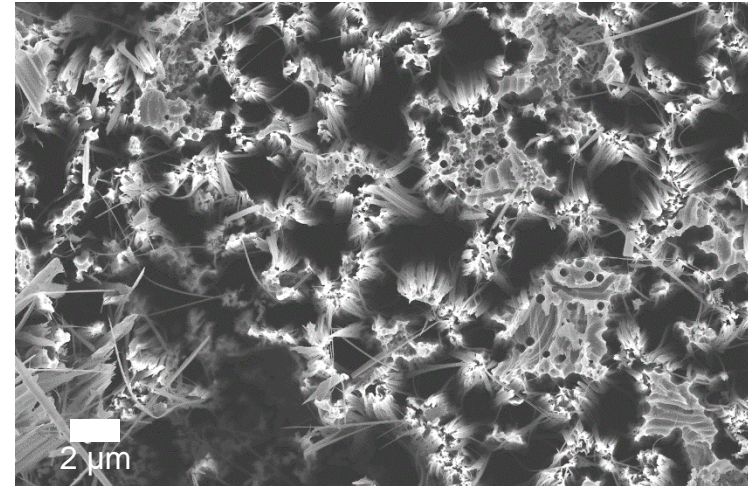
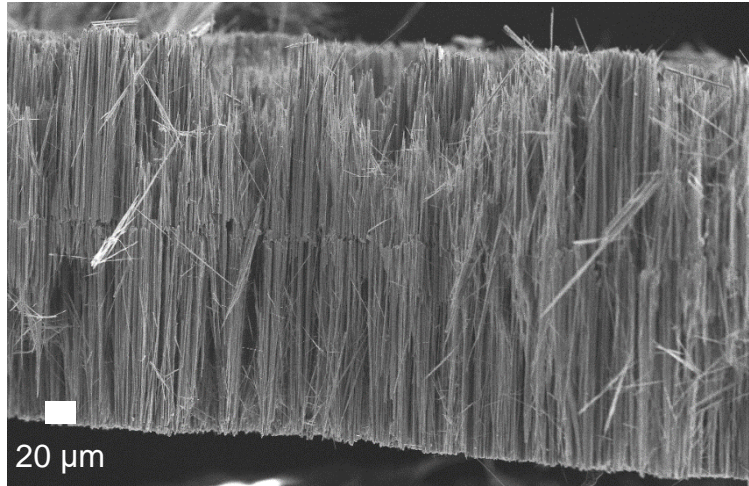
$$\kappa = 4.6 \text{ W/mK}$$



E. Dimaggio & G. Pennelli, Nano Letters 16 (2016) 4348

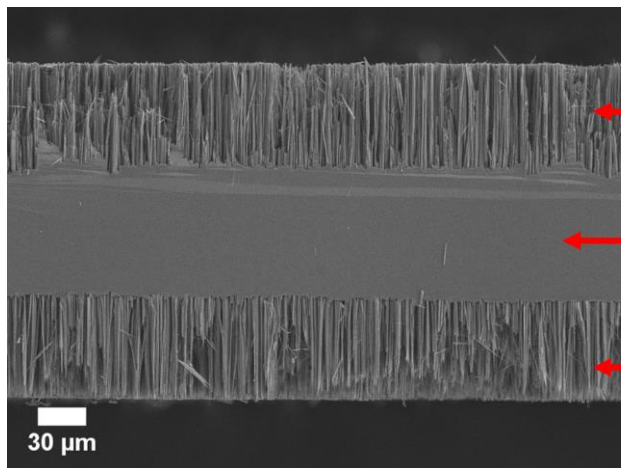
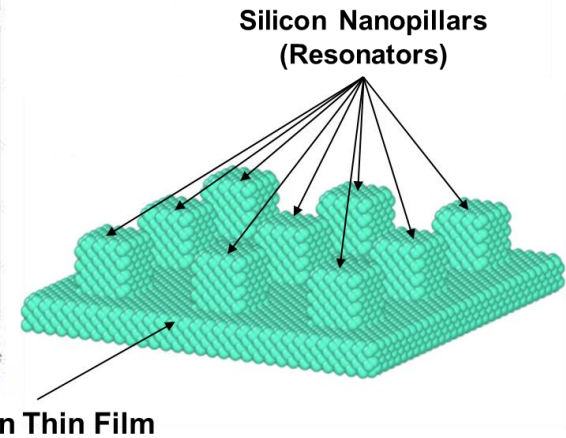
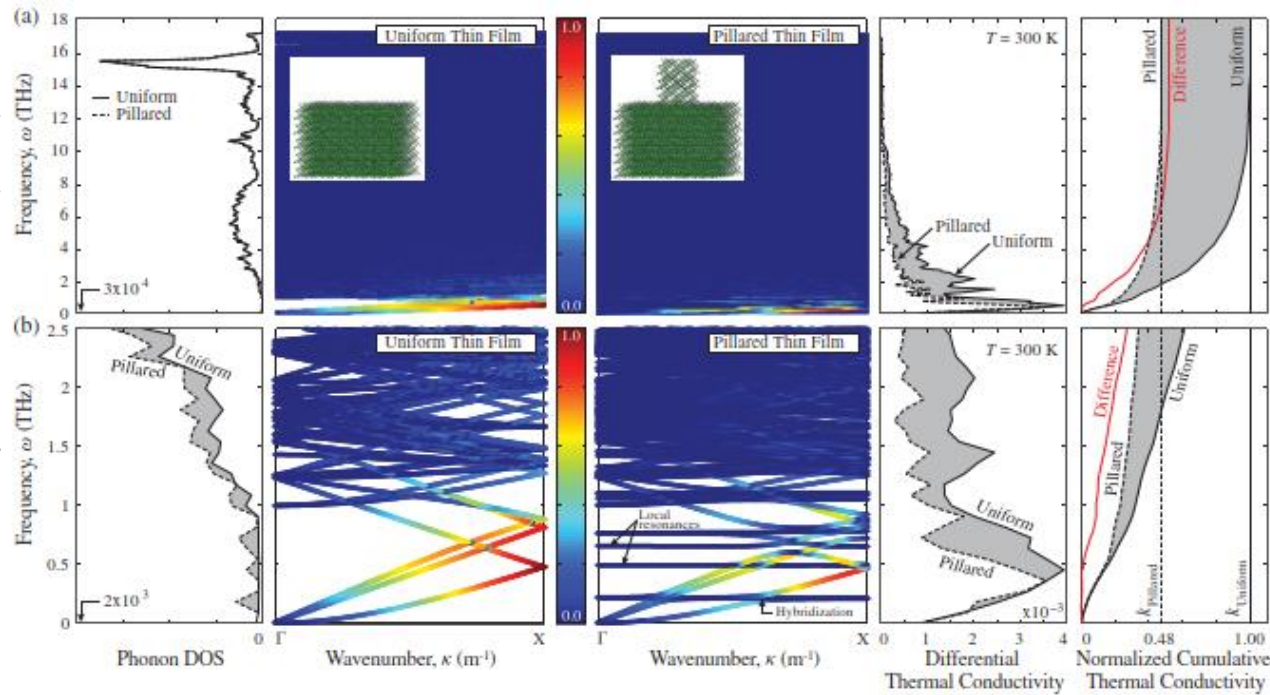
S. Elyamny et al., Nano Letters 20 (2020) 4748

Silicon at Low Temperatures: Nanowires



Silicon at Low Temperatures: Nanowires

B.L. Davis & M.I. Hussein, Phys. Rev. Lett. 112 (2014) 55505



Resonators

**Silicon Thin Film
(electron pathway)**

Resonators

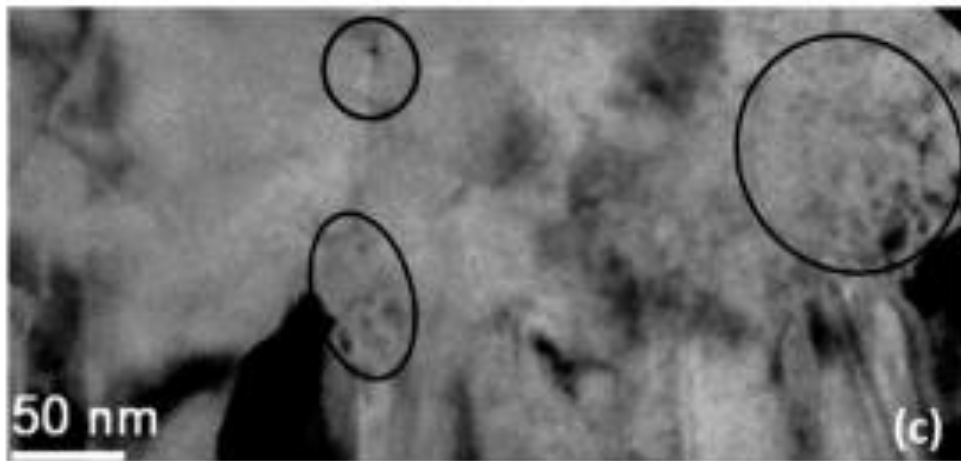
- σ and α of Si membrane (34 μm) unaltered
- κ of Si membrane reduced to 53 W/mK

Silicon at Low Temperatures: Thin Films

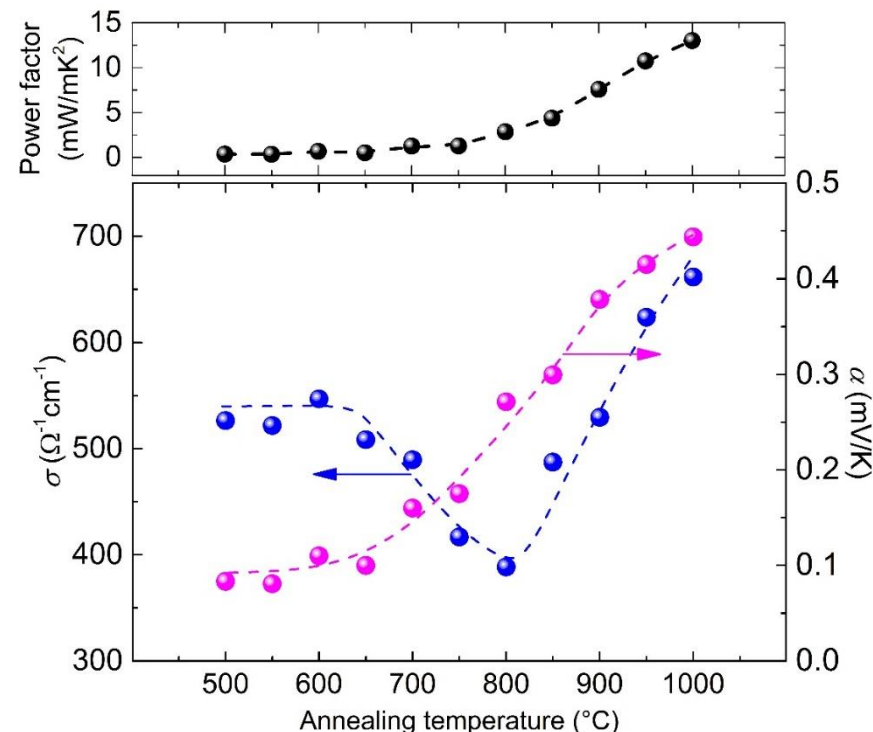
Films (220 nm) deposited by CVD at 625 °C using SiH_4 onto Si (100) | 100-nm SiO_x

Doping ($4.4 \times 10^{20} \text{ cm}^{-3}$) by I^2 (B^+ , 26 keV, $6.0 \times 10^{15} \text{ cm}^{-2}$ + 47 keV, $6.0 \times 10^{15} \text{ cm}^{-2}$), activated by RTP, 1050 °C, 40 s + thermal processing in Ar, 1000 °C, 2 hrs.

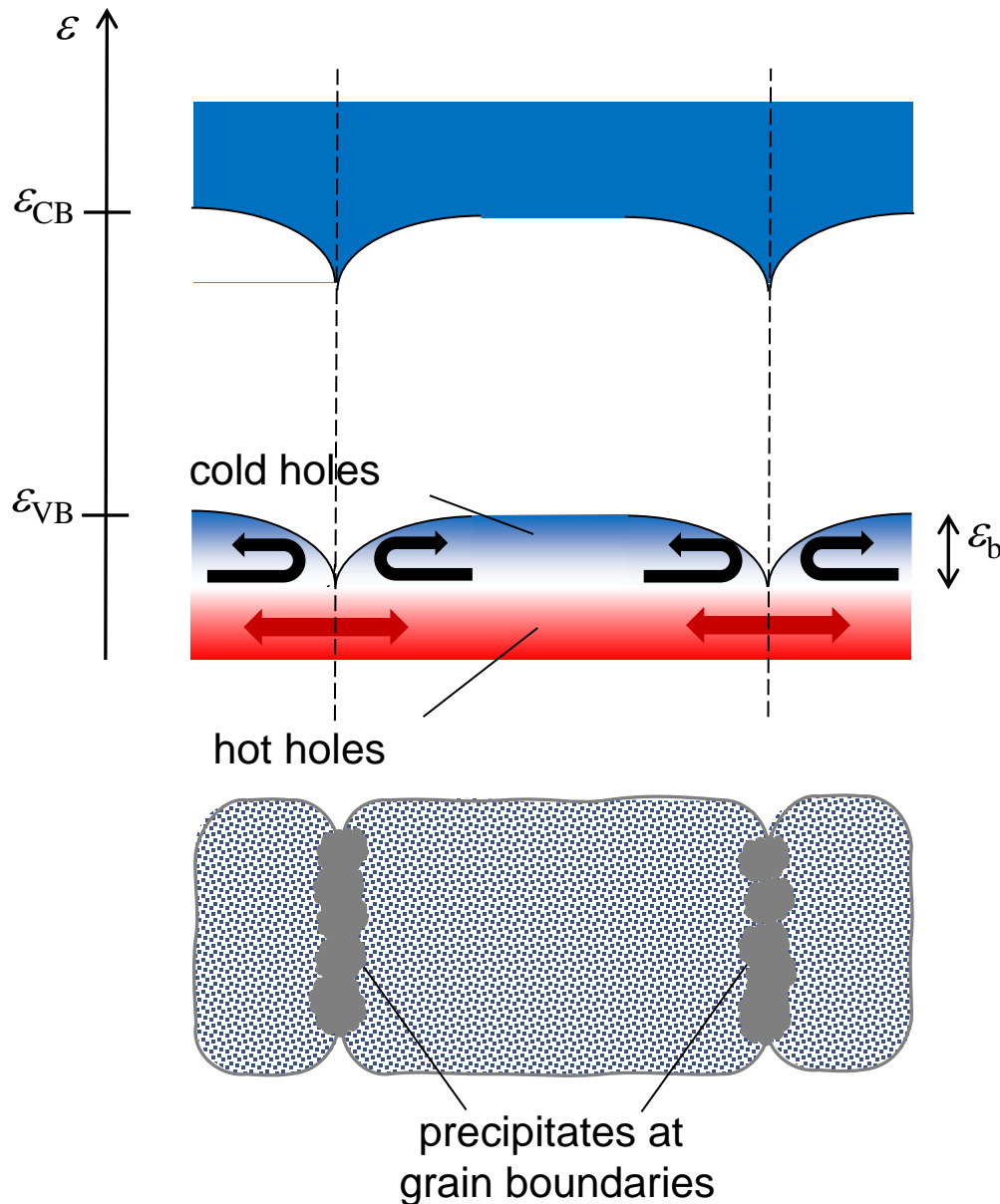
Above 800 °C, boron diffusivity is large enough to enable its migration, leading to its precipitation around GBs forming a B-rich second phase (possibly SiB_3).



DN et al., Proc. 8th ECT, Como, 2010, 141
 DN et al., J. Solid State Chem., 193 (2012) 19
 DN et al., AIP Conf. Proc., 1449 (2012) 311
 DN et al., Phys. Status Solidi A, 211 (2014) 1255
 DN, S. Frabboni, X. Zianni, J. Mater. Chem. C, 3.47 (2015) 12176



Energy Filtering in nanoSi TFs



SiB_x sets barriers at GB

Cold holes are localized

Hole density decreases, so α increases

Since only hot holes diffuse, μ increases

The enhanced μ compensates for the reduction of p

The power factor increases

For the mechanism to be effective

- carriers must not relax within grains, so grain size must be \approx MFP
- barrier height is critical

N. Neophytou et al., Nanotechnology, 24 (2013) 205402

N. Neophytou et al., J. Electron. Mater., 43 (2014) 1896

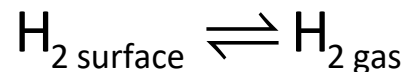
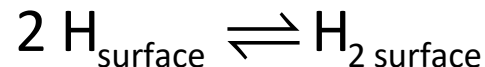
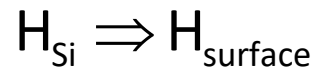
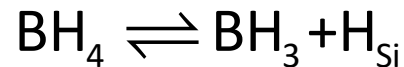
X. Zianni & D. Narducci, J. Appl. Phys., 117 (2015) 035102

X. Zianni & D. Narducci, Nanoscale, 11 (2019) 7667

N. Neophytou et al., Mater. Today Phys., 11 (2019) 100159

The Role of Hydrogen

- H remains embedded upon CVD growth
- H binds to B and dangling bonds at GBs
- Thus, H hampers B precipitation at GBs
- H presence confirmed by FTIR, with thermal processing causing its release
- Size effects in desorption processing reported, due to gas velocity at film surface

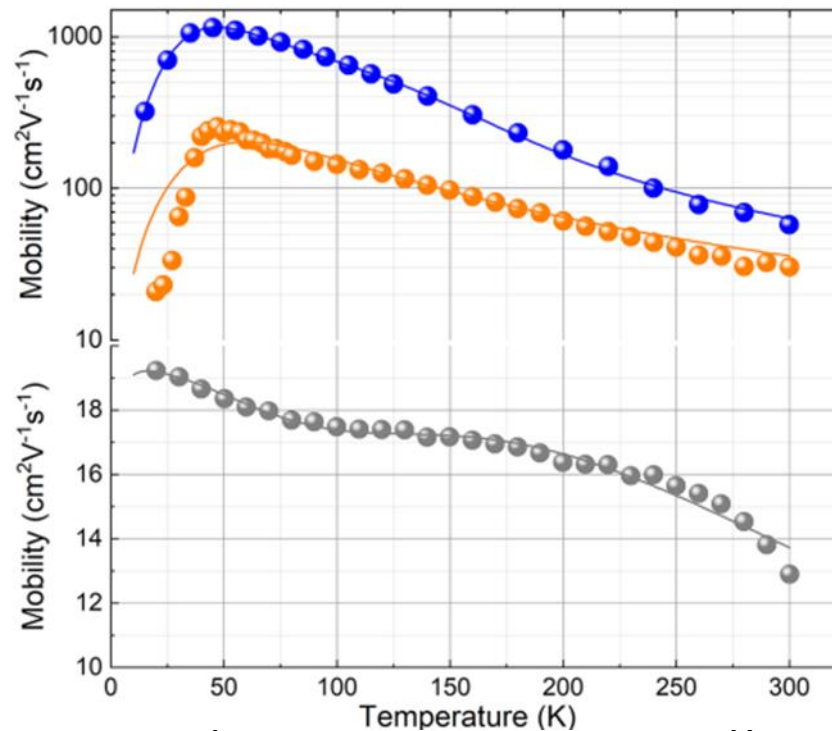


Gas desorption depends on H_2 pressure nearby the film surface

The Role of Hydrogen

- Sample aged at room temperature for 5 years

Type	σ	α	PF	Relative PF
Untreated, aged				0.69
Small, aged				23.0
Large, aged				10.5

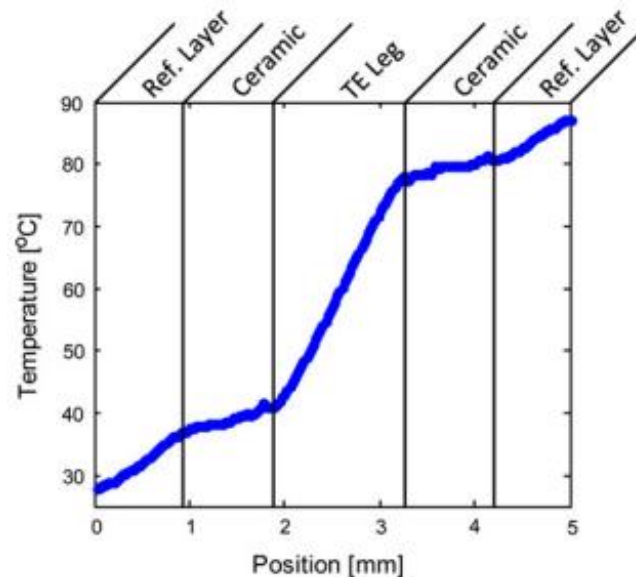
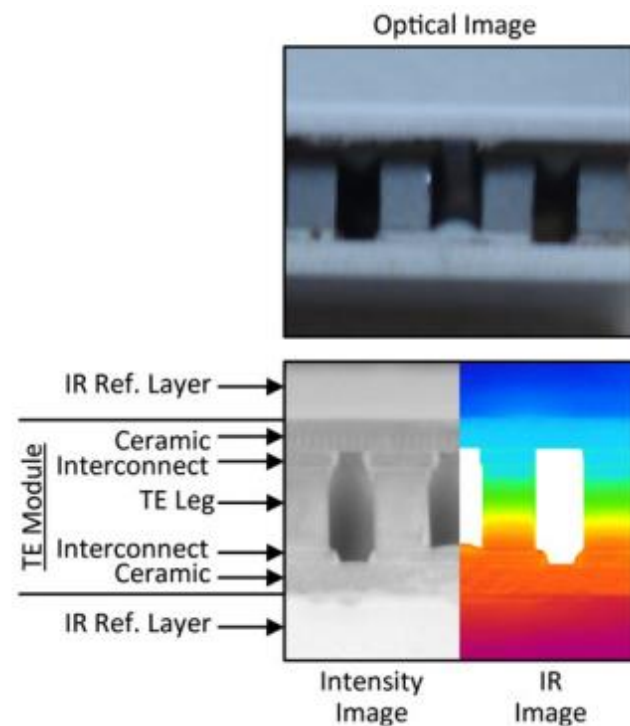


- Hydrogen had tir temperature inde
 - Partial spontane (yet depending c
 - This confirms (as is present in thin films
 - A top PF value of 33.1 mW/mK² was measured
- itions and at room
- of thermal treatments
- mplies, still hydrogen

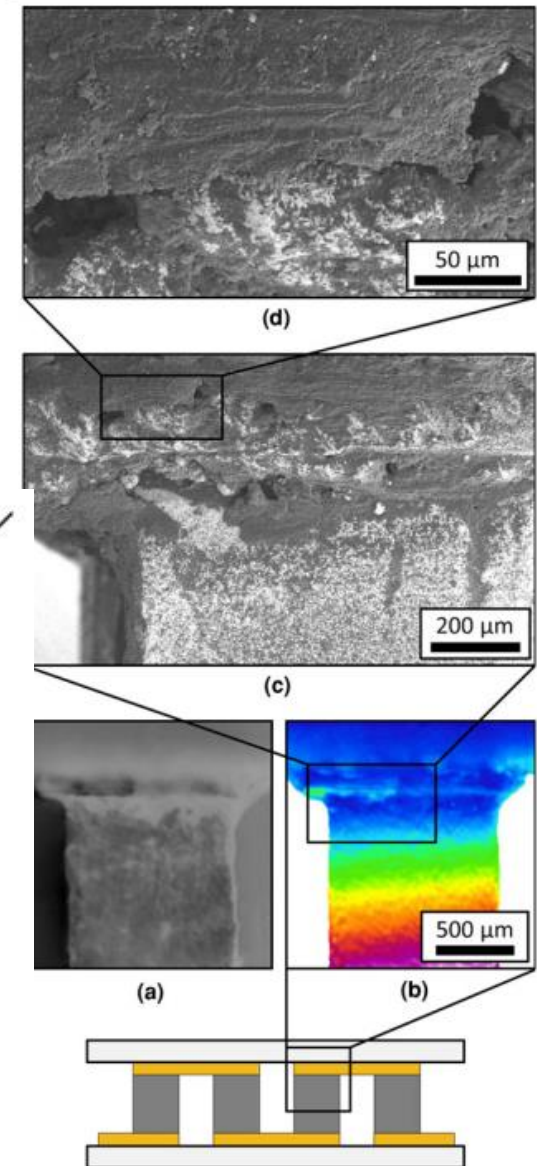
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From Materials to Devices: Reliability

- Thermal contacts rule the actual amount of ΔT sensed by the TE legs
- In contacts to soft surfaces, additional thermal resistances arise
- Furthermore, thermal cycling may cause interdiffusion at metal-TE contacts
- Reliability issues often related to metallurgy



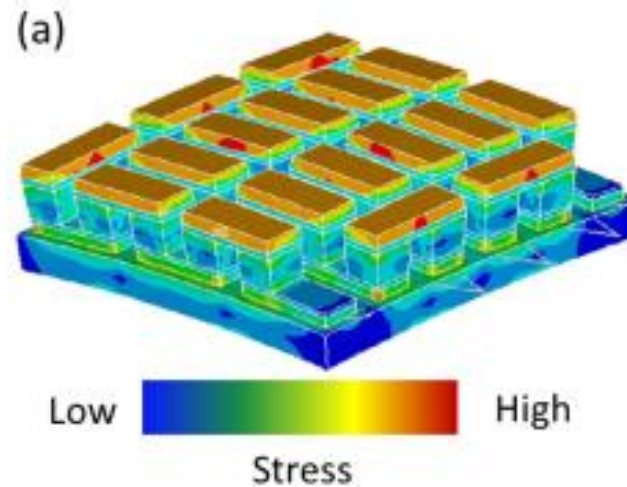
BARAKO ET AL., *J. ELECTRON. MATER.*, 42, 2013, 312



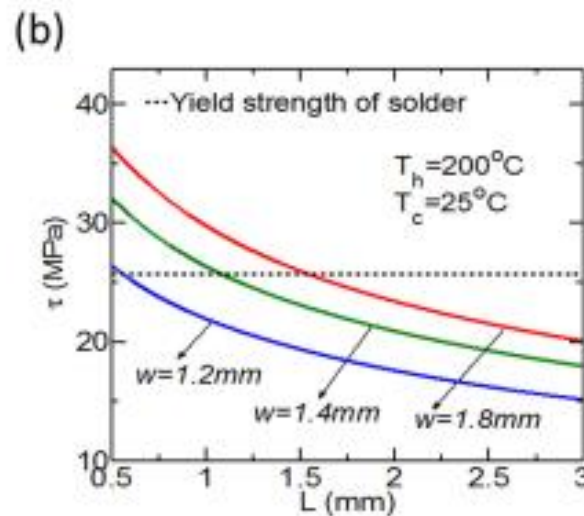
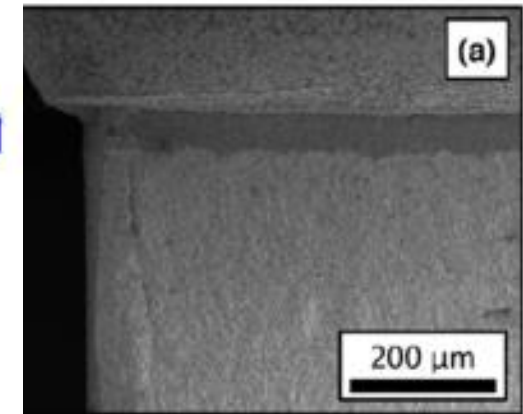
From Materials to Devices: Reliability

Low thermal conductivity causes large temperature *gradients* to develop for any given heat flux

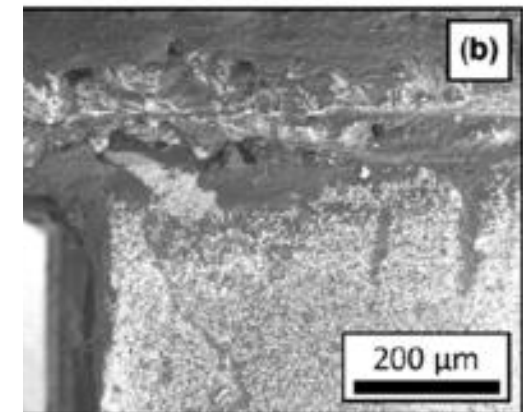
This often enhances issues related to different CTE of materials, including interface stress



Before Thermal Cycling



After Device Failure



W. Liu et al., Scripta Mater. 111, 3 (2016)

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Applications



RTG for *pacemakers* (USA, 1974)



Temp scavenger (USA, 1974)



Watch powered by body heat (Japan, 1998)

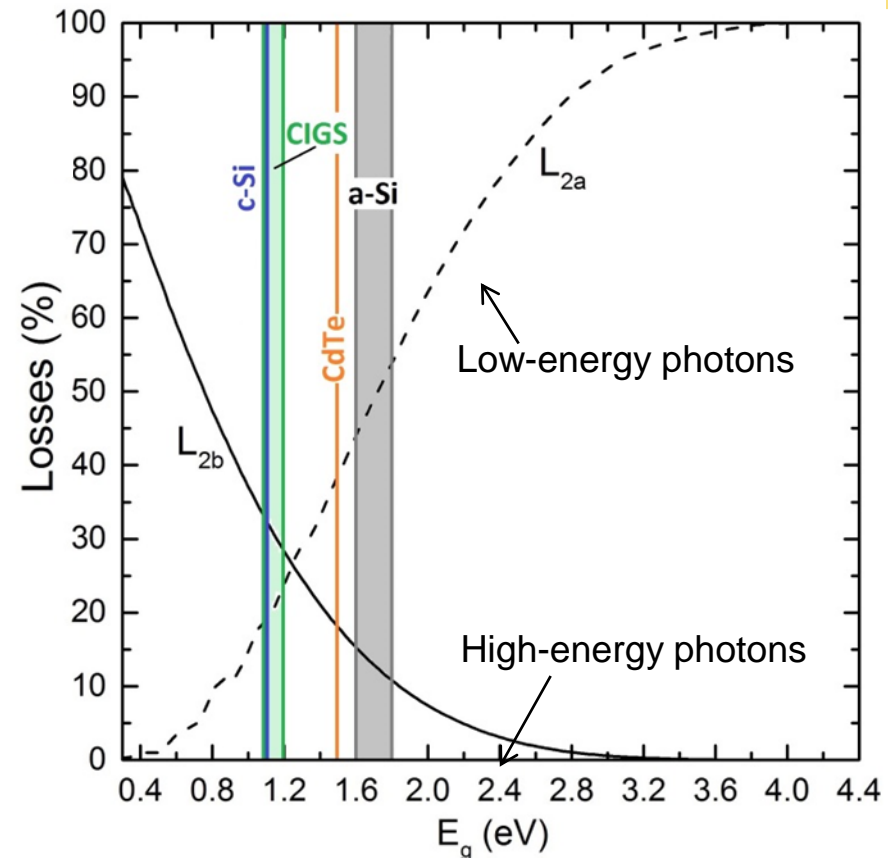
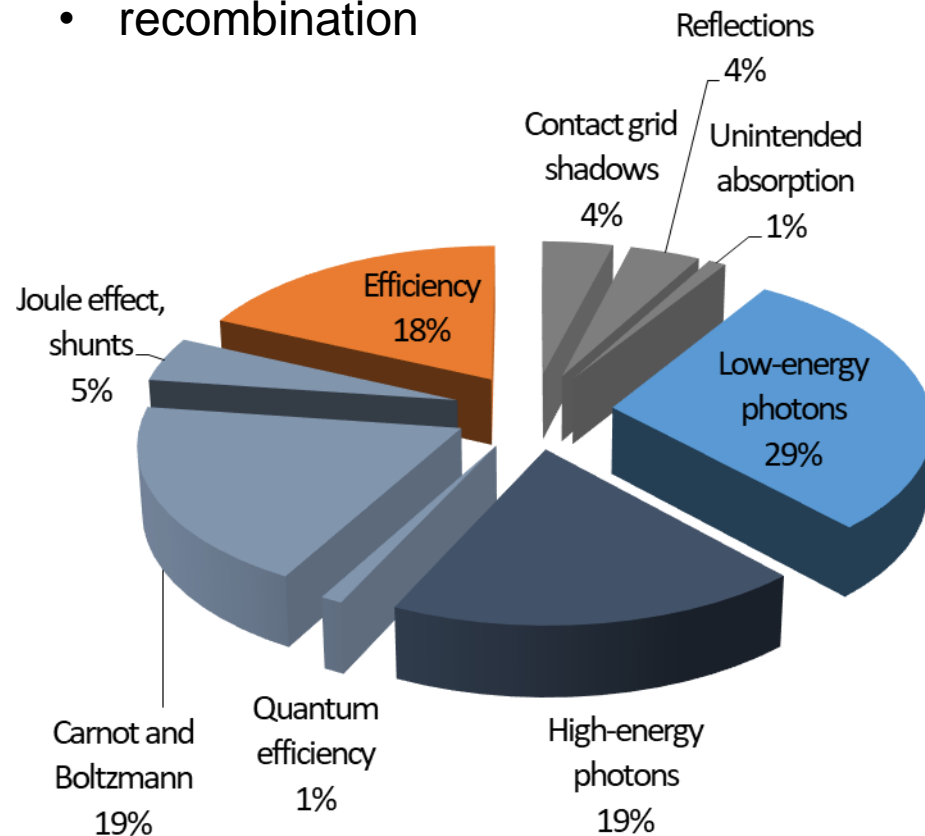


Car muffler scavenger (Europe, 2005)

Applications: Co-generation (HTEPV)

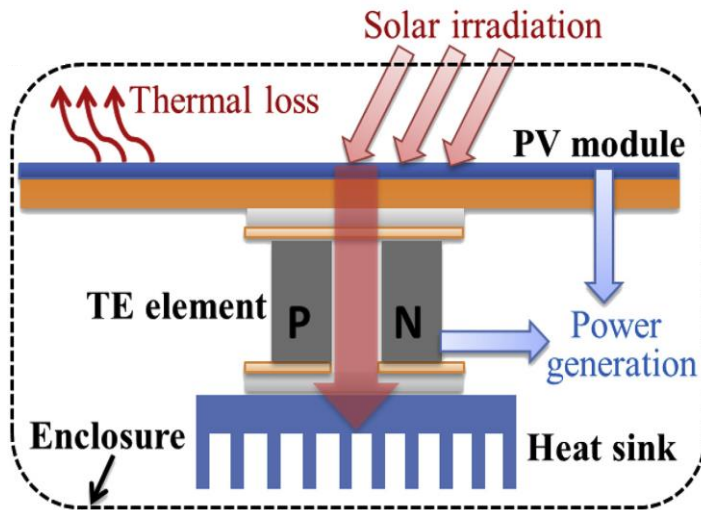
PV efficiency is mainly limited by:

- loss of photons with $\nu < E_g/h$
- thermalization of photons with $\nu > E_g/h$ (also degrading PV efficiency)
- recombination



This mostly results in a production of heat that must be dissipated (to prevent η_{PV} degradation) but that might be also reused in TEGs

Applications: Co-generation (HTEPV)

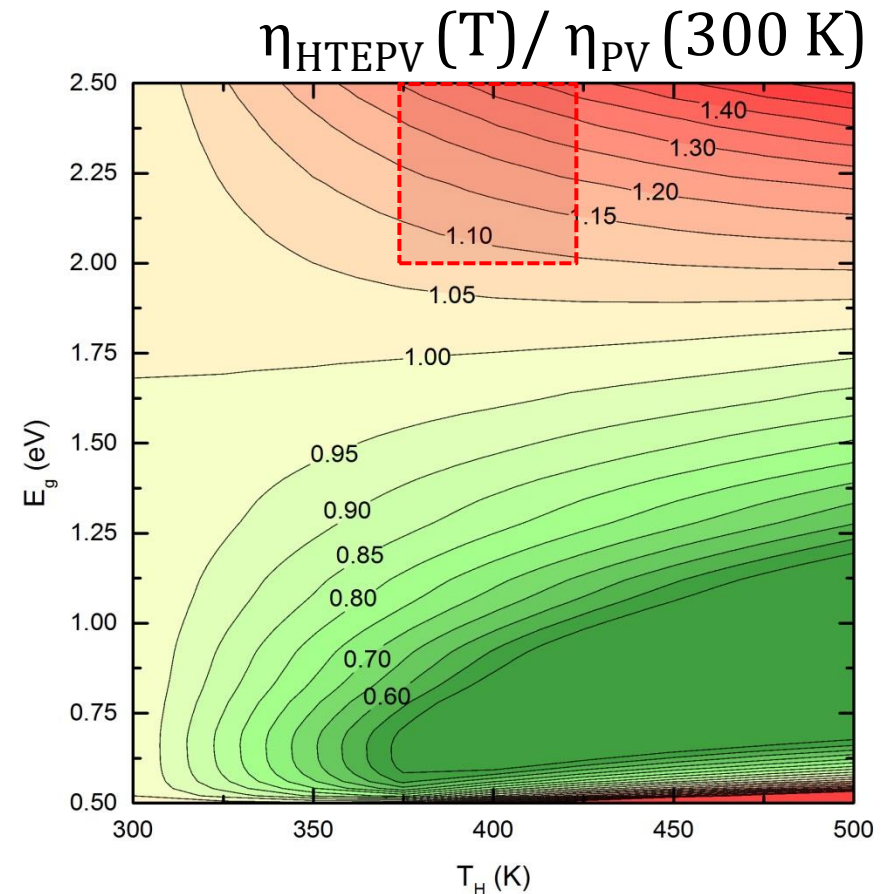


W. Zhu et al., *Energy*, 100, 2016, 91.

‘Upward’ reflective losses at PV surface
Heat mirror needed, transmitting radiation
above the gap and backreflecting in the
IR region.

Typical HM materials are oxides (TCO,
ITO, etc.)

B. Lorenzi & G. Chen, *J. Appl. Phys.*, 124 (2018) 024501

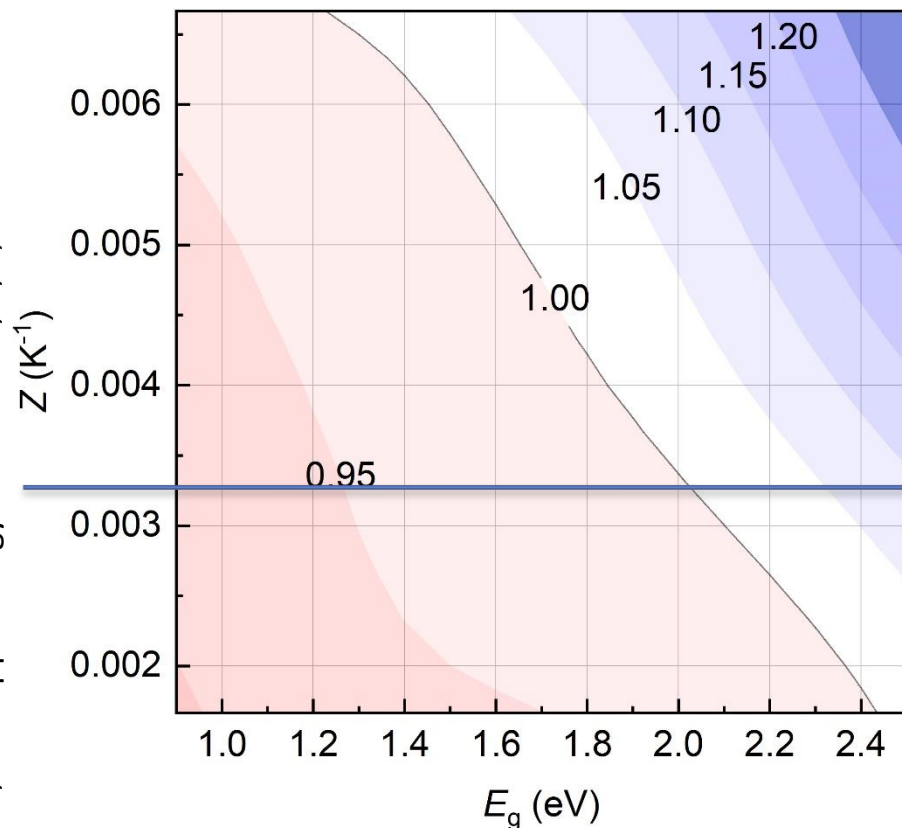


B. Lorenzi et al., *J. Electron. Mater.*, 44 (2015) 1809

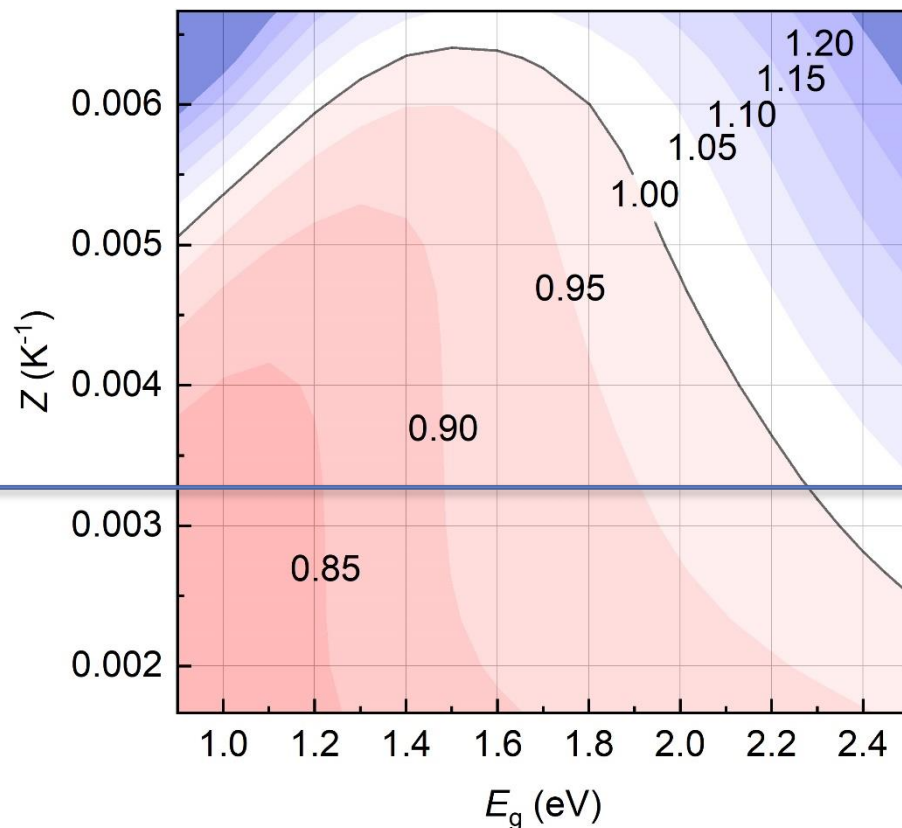
B. Lorenzi et al., *J. Mater. Res.*, 30 (2015) 2663

Applications: Co-generation (HTEPV)

Low ERE (10^{-6})



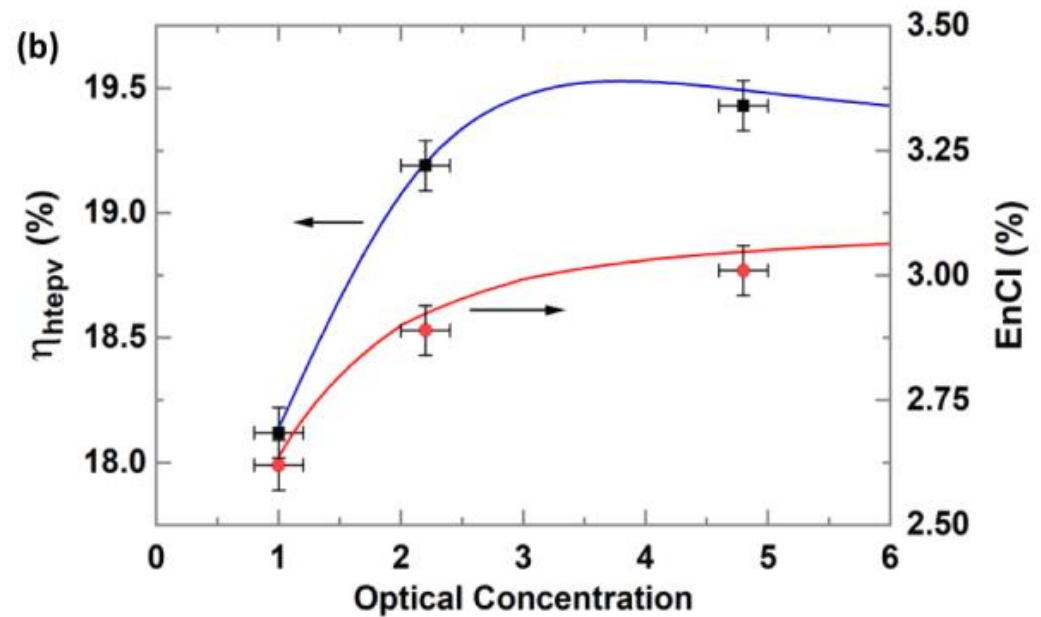
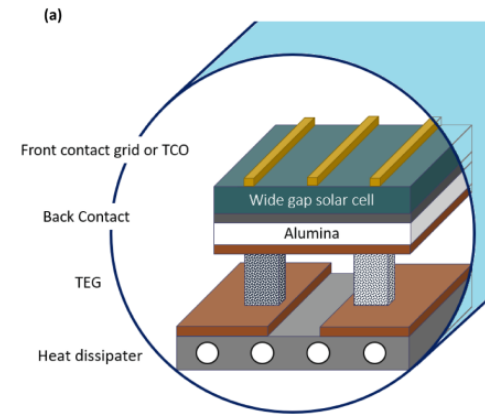
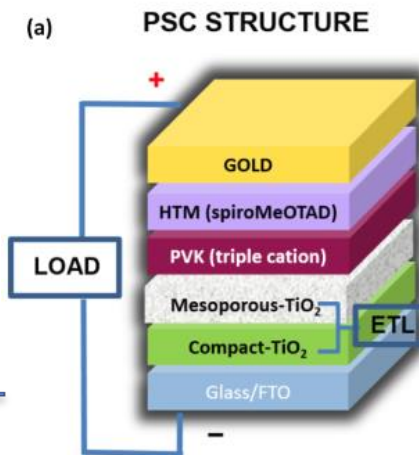
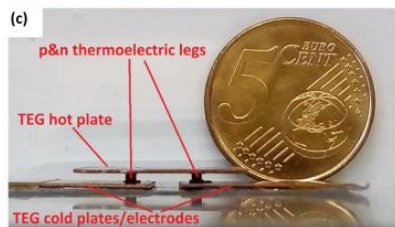
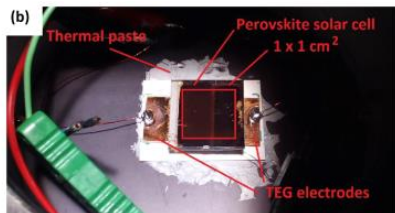
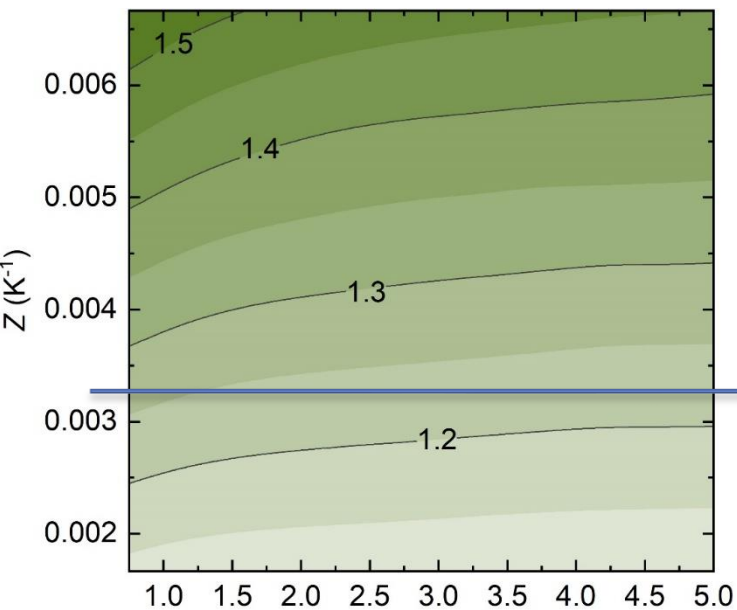
High ERE (10^{-2})



Economic analysis shows that

- neither concentrated or moderately concentrated HTEPVs are profitable for $zT \approx 1$ and E_g in the standard range 0.8-1.5 eV
- TE pairing with PV may be suitable to promote low-cost «poor» PV materials (such as a-Si, $\mu\text{c-Si:H}$)

Applications: Co-generation (HTEPV)



Applications: Microgeneration

In 2006, devices autonomously exchanging information have outnumbered humans connected to Internet worldwide.

IoT is often populated by remotely deployed devices, so that sensing nodes need not only to exchange data wirelessly but also to operate maintenance-free over their lifetime.

Either energy sources or renewable energy converters must be then embedded in the sensor.



Applications: Microgeneration

TEG competition with batteries must be evaluated as of:

- energy requirements, comparing battery energy storage with energy demand of services sensing nodes
- power requirements, comparing the electric power a TEG can generate to the power demand of sensing nodes
- economic competitiveness, comparing power and energy costs of TEGs and batteries



Cost models

Batteries

Type	Specific energy (J/g)	Specific Power (W/g)	Energy cost (USD/MJ)
Lead acid	134	0.18	40
NiCd	176	0.15	119
NiMH	305	0.5	119
NiZn	360	3.0	113
LiCoO ₂	587	0.29	152
LiFePO ₄	358	2.4	152

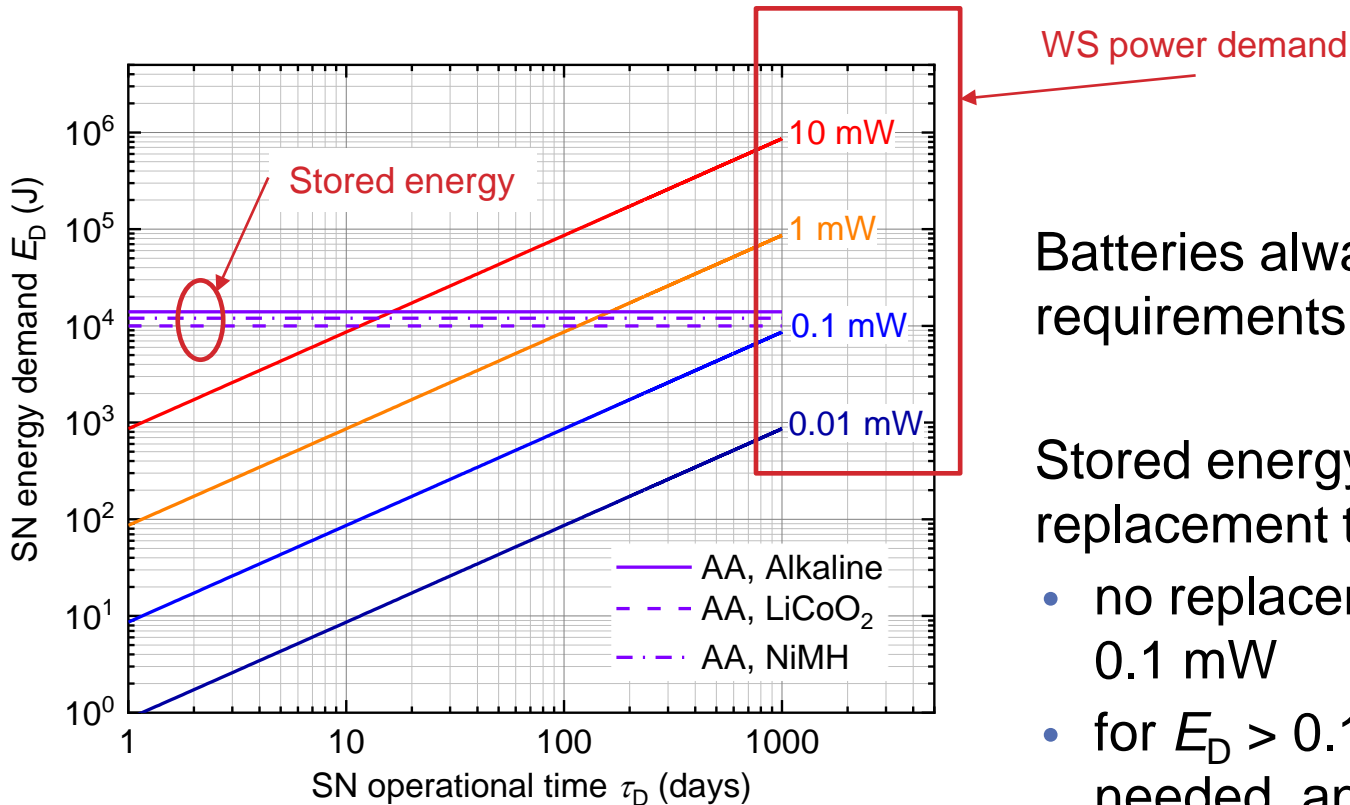
TEGs

For bulk TEGs

- optimized power costs currently ≈ 38.5 USD/W
- device *costs* for commercial TEGs ≈ 5.6 USD (bulk *prices* ≈ 25 USD)

For microTEGs (MEMS cost model)

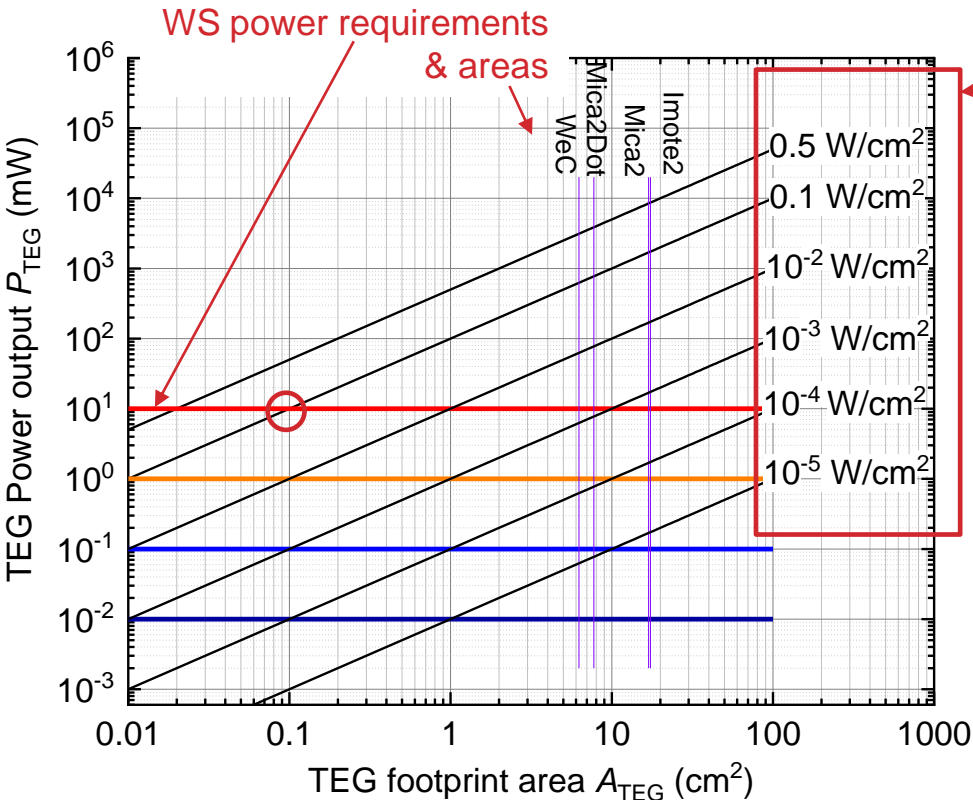
- devices costs depend on litho steps but ruled by packaging
- range from 1.03 USD/cm² (1L) to 1.48 USD/cm² (5L)
- estimated power costs from 60 USD/W (1L) to 120 USD/W (5L)

Energy demand

Batteries always meet *power* requirements.

Stored energy sets instead replacement times:

- no replacement needed for < 0.1 mW
- for $E_D > 0.1$ mW, replacements needed, and costs must be accounted for

Power demand

TEG power densities

TEGs have no *energy* constraints, being harvesters

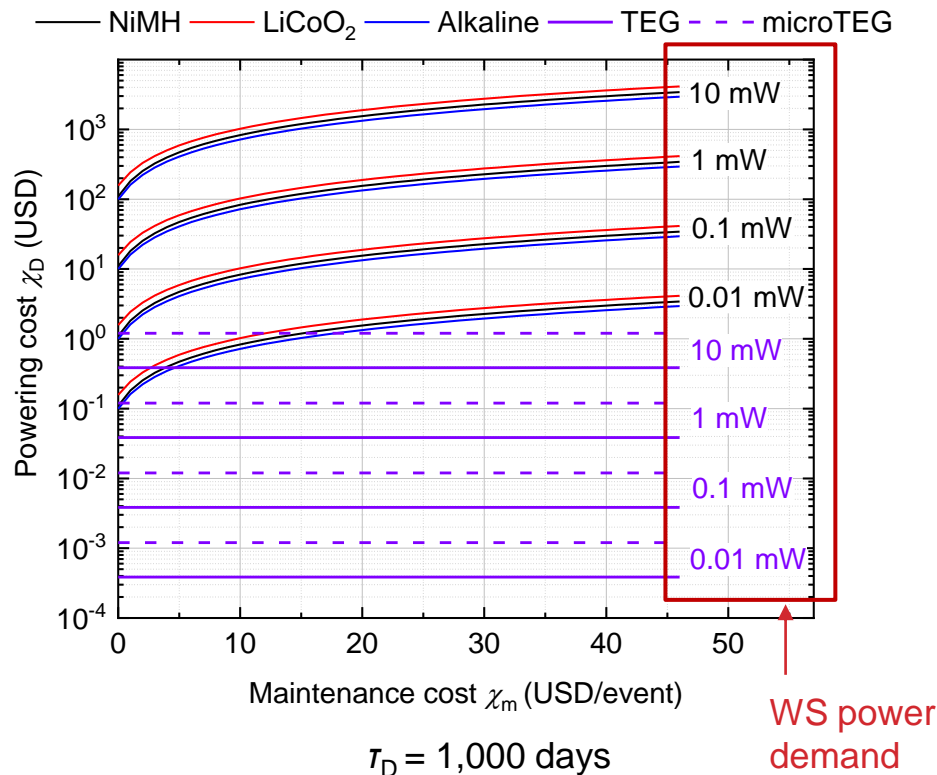
Cross-points set minimal TEG areas

- MicroTEGs may service WSs with power demands $< 0.1 \text{ mW}$ only
- Bulk TEGs provide enough power to suit any WSs, even when accounting for thermal chain inefficiency/lower ΔT

Power limitations for TEGs are therefore less stringent than possibly expected. Competitiveness is set by economic factors.

Comparison: Powering costs

Powering Costs



Economic metrics for batteries are USD/J (C_b) while for TEGs are USD/W (c_{TEG}). Thus, both WS lifetimes τ_D and replacement costs χ_m matter.

Note that a WSN requiring 1 mW over 1,000 days imply a battery powering cost of 9.36 USD + maintenance vs. < 0.12 USD if TEGs are used

Replacement costs depend on labor cost (5 to 23 USD/h) and duration (10 mins to 2 h): 1 to 46 USD/event.

Some Conclusions

- Research on thermoelectrics joins great fundamental challenges on materials and transport properties with applications
- Effort to develop nanomaterials has contributed to a deeper understanding of transport phenomena also at the macroscale
- Heat harvesting will remarkably contribute to the Green transition
- Low temperature micro and distributed generation are the closest area of exploitation
- Thermal management/cooling are key enabling technologies to ULSI



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M. Arcari



S. Magagna



B. Lorenzi



E. Villa



F. Giulio

Credits



Neophytos Neophytou



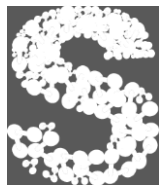
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Ahmed Charai
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Claude Alfonso
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Domenique Mangelinck
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FP7-NMP-2013-SMALL-7
SiNERGY Project,
Contract n. 604169



Sandro Solmi Alberto Roncaglia
Matteo Ferri Francesco Suriano
Fulvio Mancarella Luca Belsito
Francesco Moscatelli



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NANOthermMA Project
European Union's Horizon 2020
Grant Agreement No. 678763



Size & Aging Effect

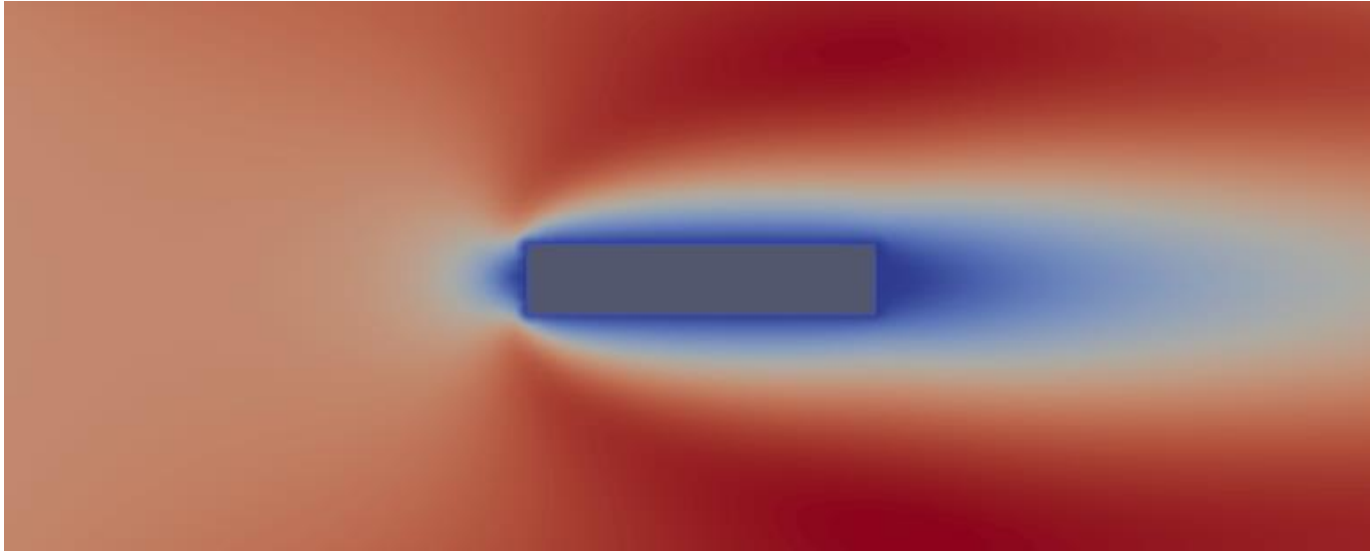
Film characteristics after thermal processing were found to depend upon their size. Large samples systematically reported no PF enhancement.

Type	σ ($\Omega^{-1}\text{cm}^{-1}$)	α (mV/K)	PF (mW/m ² K)	Relative PF
Untreated	562	0.16	1.44	1
Small (5x50 mm ²)	544	0.55	16.5	11.4
Large (25x100 mm ²)	169	0.23	0.89	0.62
Wafers (200 mm dia.)	223	0.21	0.98	0.68

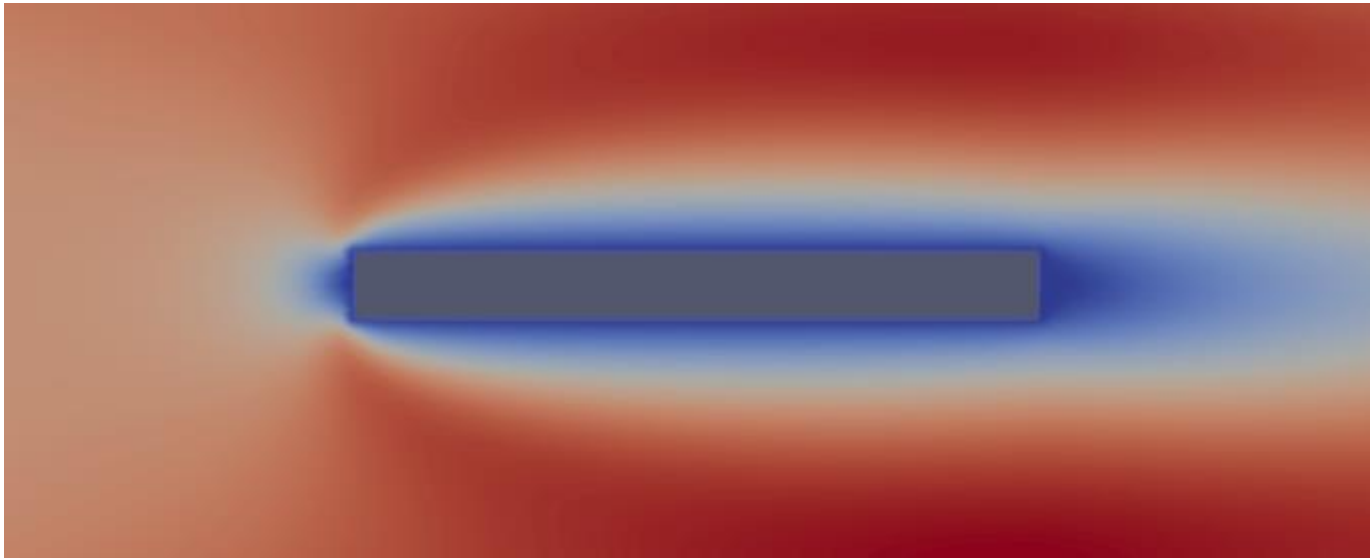
Furthermore, an additional enhancement of PFs after thermal processing in aged samples

Type	σ ($\Omega^{-1}\text{cm}^{-1}$)	α (mV/K)	PF (mW/m ² K)	Relative PF
Untreated, aged	556	0.13	1.00	0.69
Small, aged	588	0.75	33.1	23.0
Large, aged	357	0.65	15.1	10.5

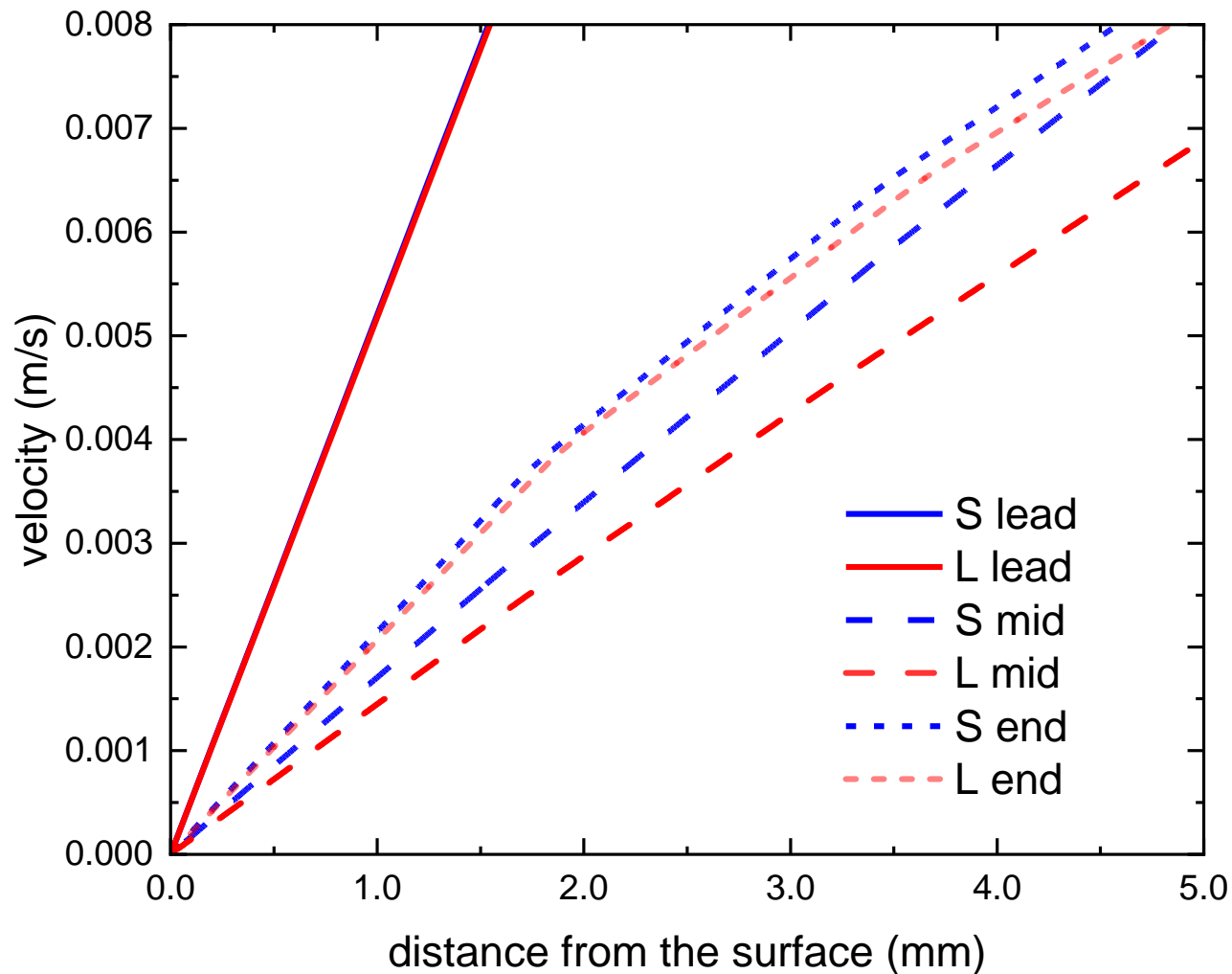
The Role of Hydrogen



Flux: $4.26 \times 10^{-6} \text{ m}^3/\text{s}$
Velocity @ 1000 °C:
 $1.44 \times 10^{-2} \text{ m/s}$



The Role of Hydrogen



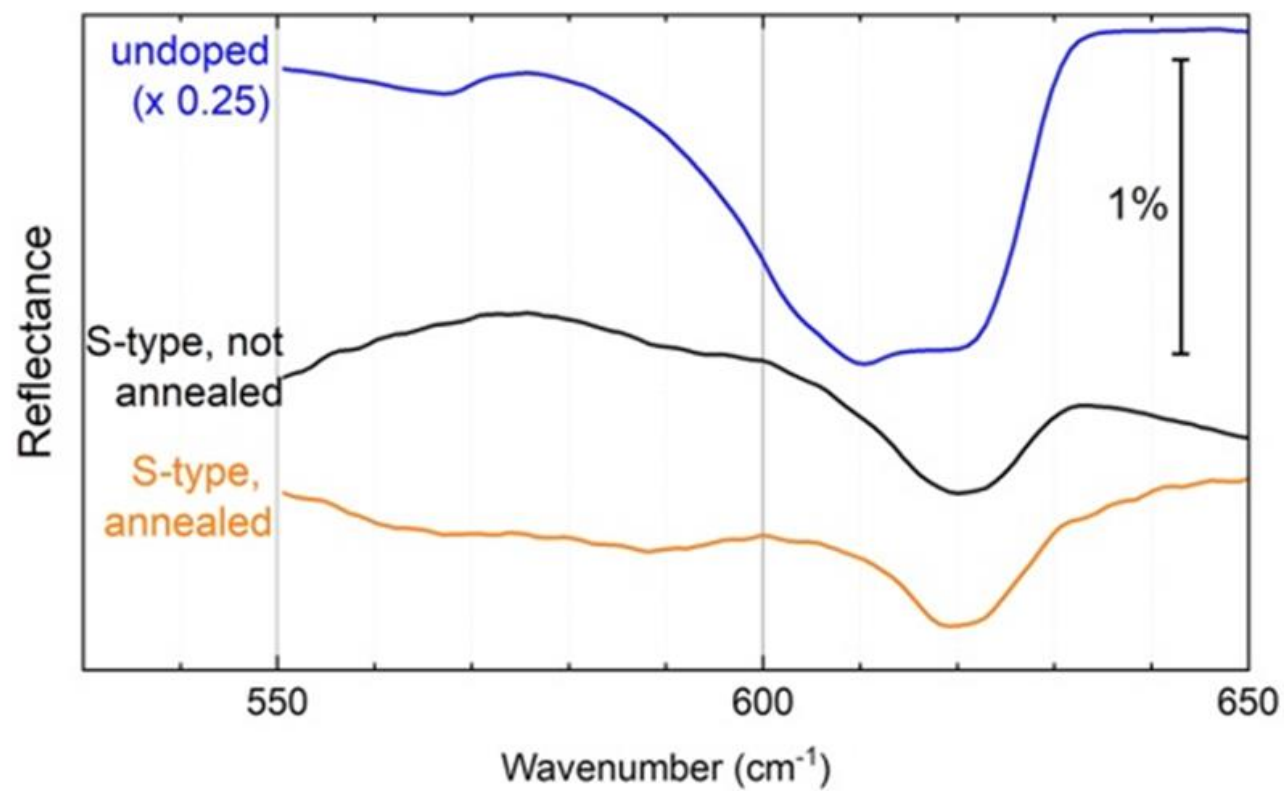
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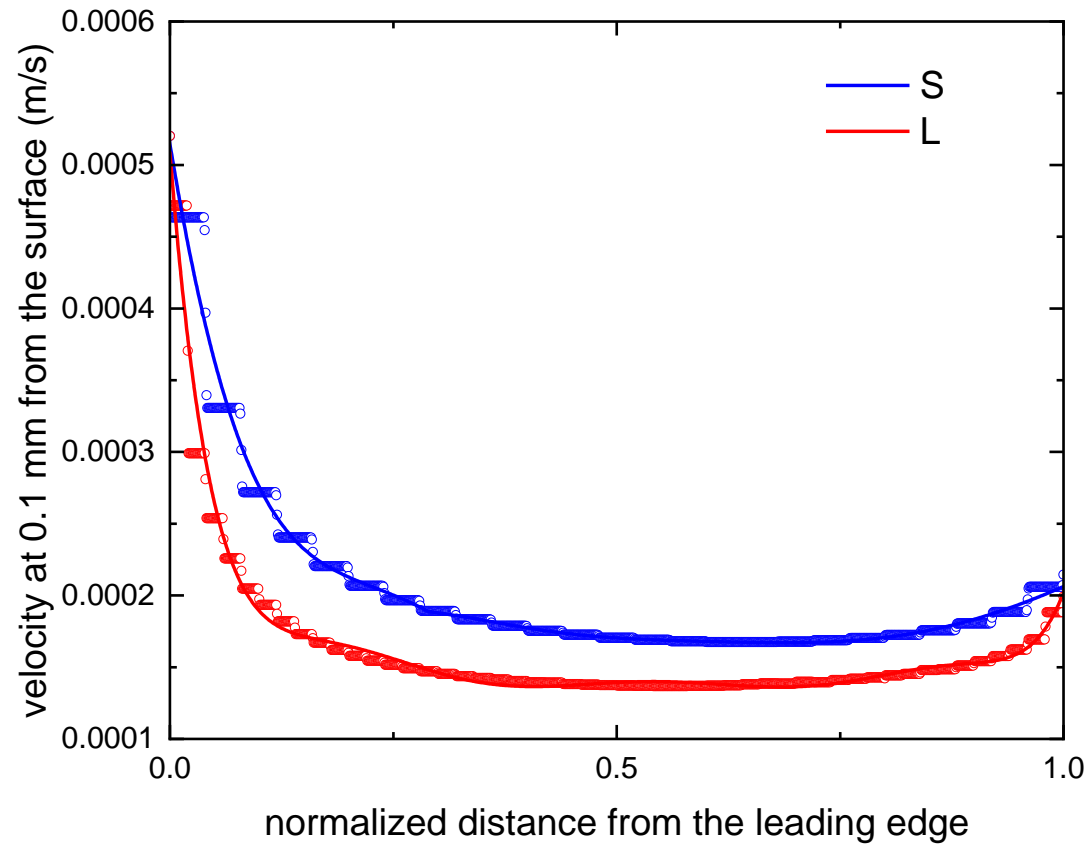
The Role of Hydrogen

To corroborate the hypothesis, thermal processing under a tripled gas flux was performed, enabling the same velocity at film surface.

Type (tripled flux)	σ ($\Omega^{-1}\text{cm}^{-1}$)	α (mV/K)	PF (mW/m ² K)	Relative PF
Small (5x50 mm ²)	626±34	0.545±0.05	18.5±5.5	12.80±3.8
Large (25x100 mm ²)	585±31	0.63±0.06	23.4±7.0	16.25±4.9

The importance of sample size may explain why no evidence of energy filtering was reported in the past on nanosilicon thin films (grown on wafers)



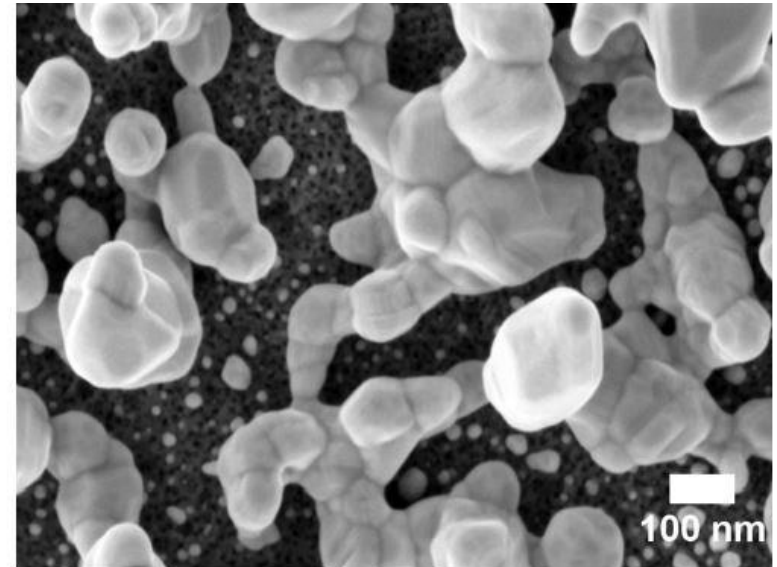
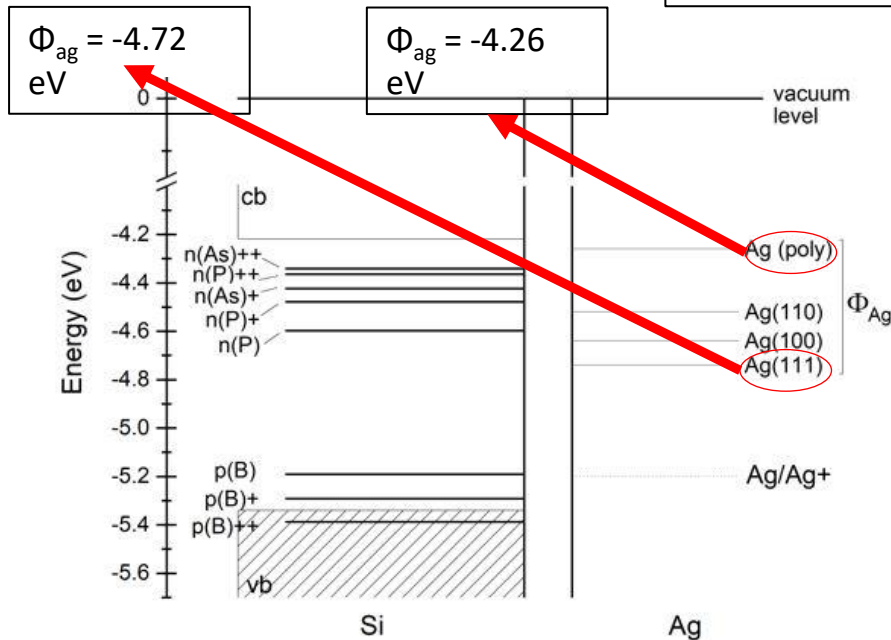


Ruling out substrate effect

- test **back-to-front current-voltage** characteristics, to test whether substrates and films are short-circuited
- switch the **substrate type**, using both n- and p-type substrates with various doping levels. No effect is observed on either Seebeck or resistivity, before or after annealing
- enhancements of the PF upon annealing at 1000 °C are **not always observed**. Systematic lack of enhancement in large samples can be hardly justified by lack of short circuits, as the size difference is by a factor 3 only
- when trying to replicate on **n-type Si thin films** (doping with P) we failed. In no case did the annealing lead to a change of Seebeck, resistivity or PF.

Silver-assisted Chemical Etching (SaCE)

Hole Exchange



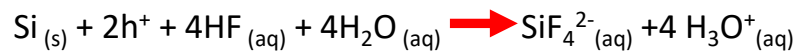
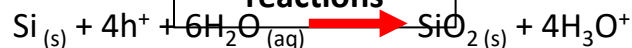
S. Magagna, D. Narducci, C. Alfonso, E. Dimaggio, G. Pennelli, A. Charaï, **Nanotechnology**, 31 (2020) 404002.

Silver-assisted Chemical Etching (SaCE)

Cathodic reaction



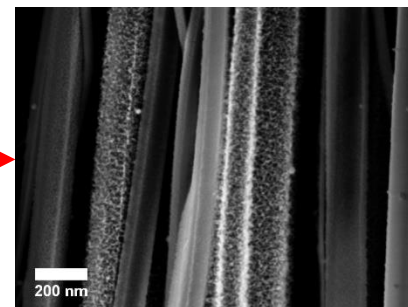
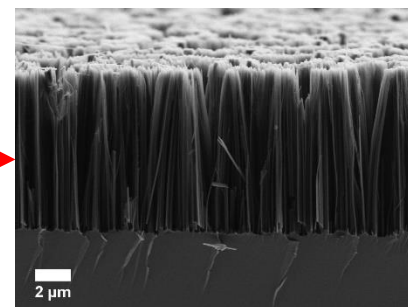
Anodic reactions



Hole Exchange

4-electron process
(electropolishing)
Pristine Si NW
formation (if
localized)

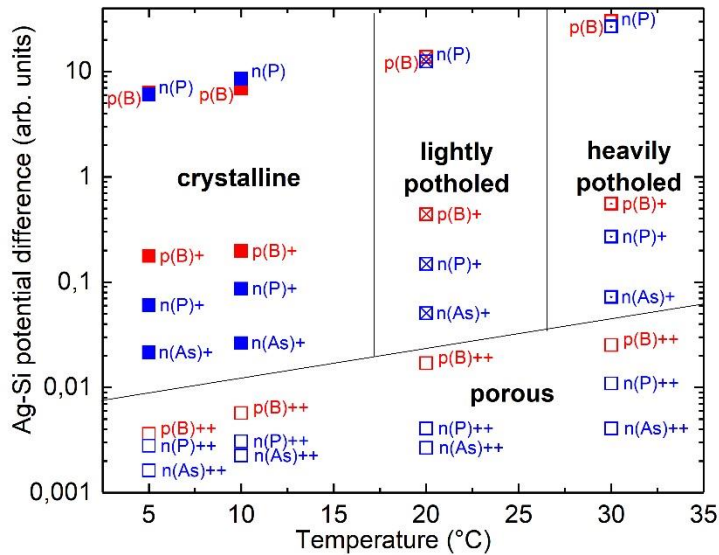
2-electron reaction
Porous Si formation
(porous NWs when
localized)



Wang et al., Adv. Mater. Interfaces (2018), 5, 1801132

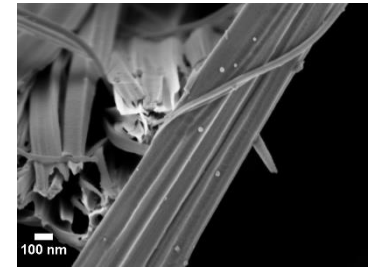
Silver-assisted Chemical Etching (SaCE)

Hole Exchange



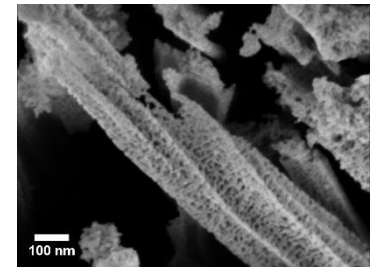
High Potential

Oxide dissolution is the **slow** reaction step



Low Potential

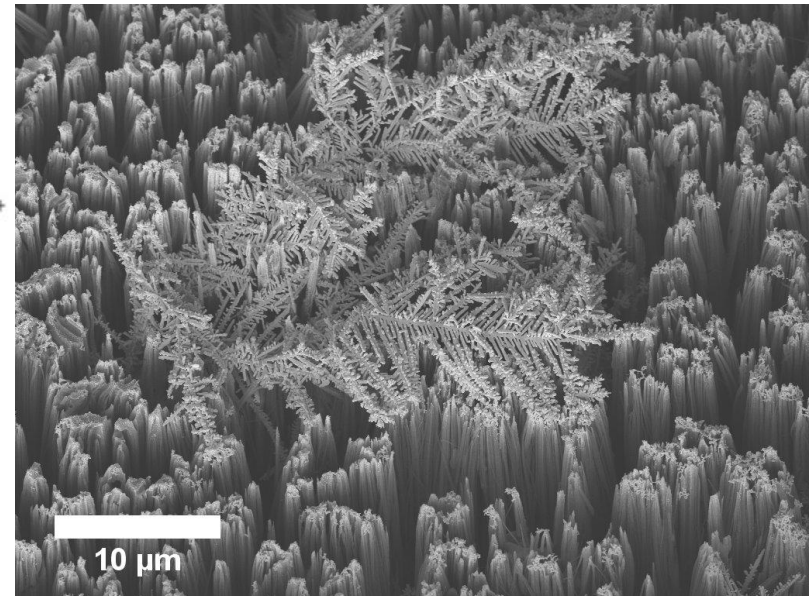
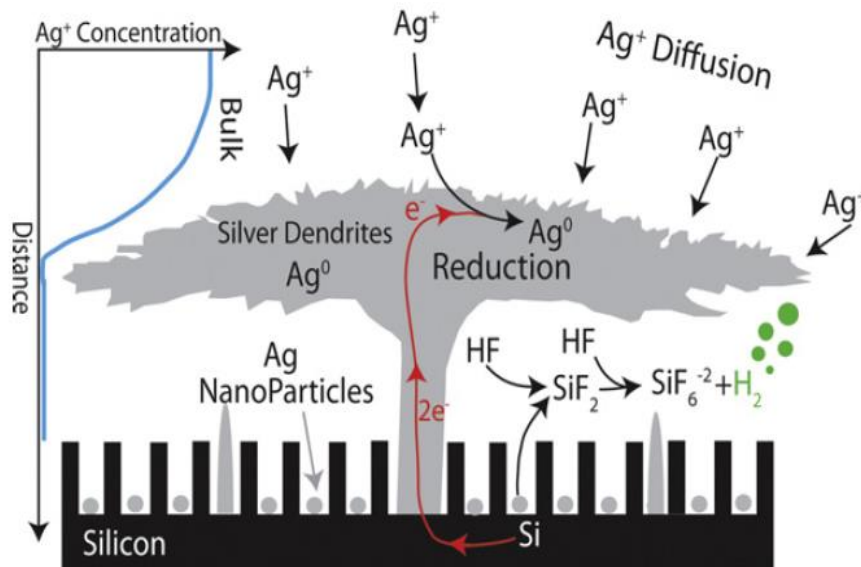
Oxide dissolution is the **fast** reaction step



S. Magagna, D. Narducci, C. Alfonso, E. Dimaggio, G. Pennelli, A. Charaï, **Nanotechnology**, 31 (2020) 404002.

Silver-assisted Chemical Etching (SaCE)

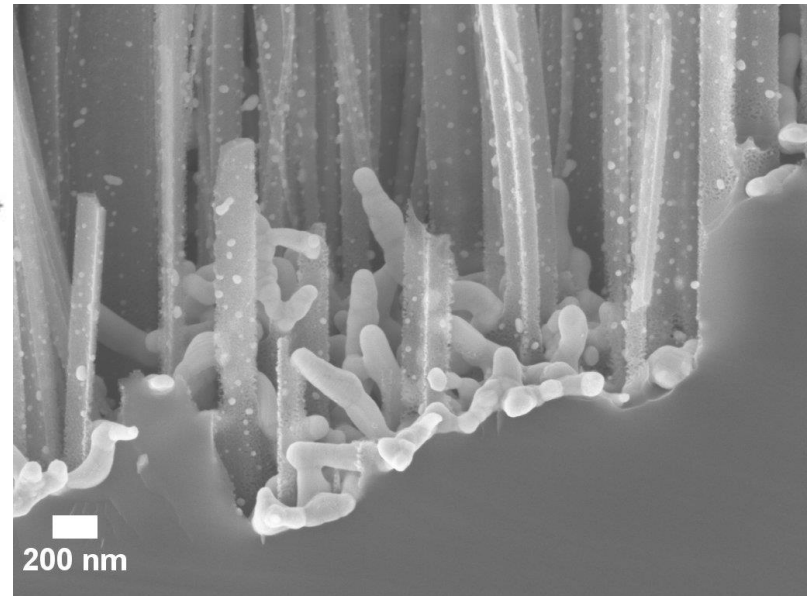
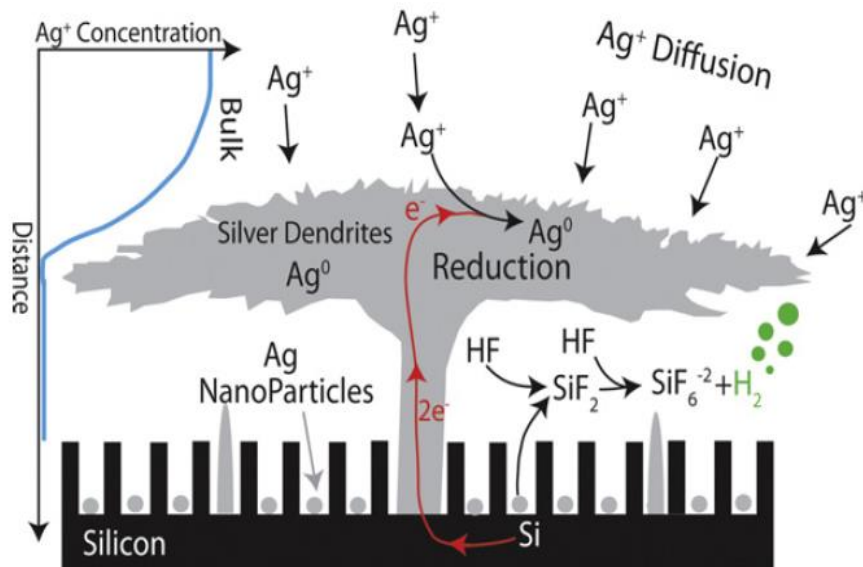
Etching Localization



Smith et al., *Electrochimica Acta* 92 (2013) 139– 147

Silver-assisted Chemical Etching (SaCE)

Etching Localization



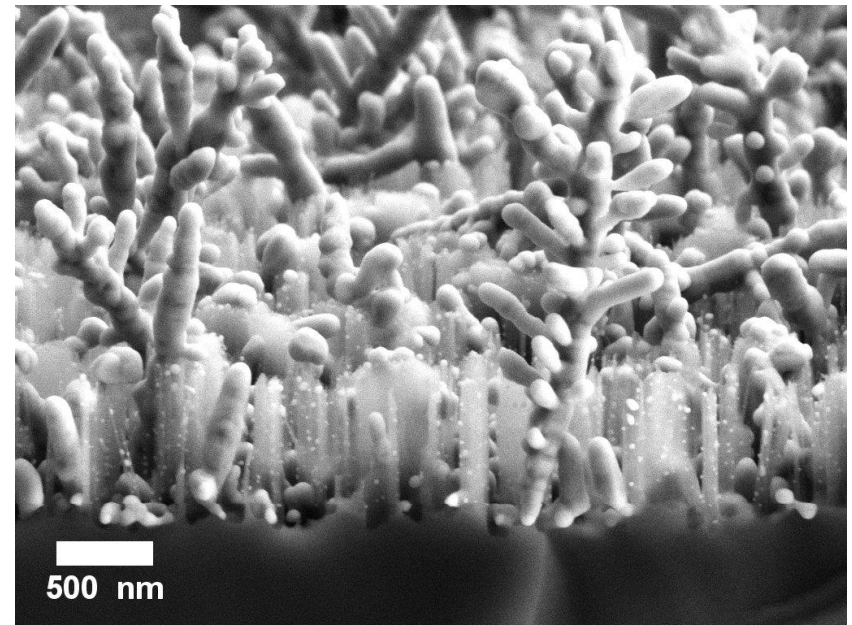
Smith et al., *Electrochimica Acta* 92 (2013) 139– 147

Silver-assisted Chemical Etching (SaCE)

Etching Localization

Lateral Bores Protection

- Etching rates are identical at all {100} surfaces (on (100) silicon substrates)
- bores are overfilled by Ag dendritic structures

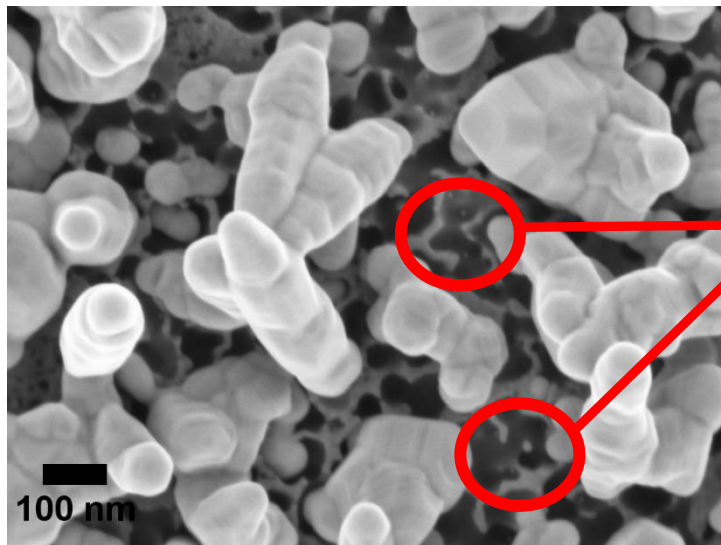


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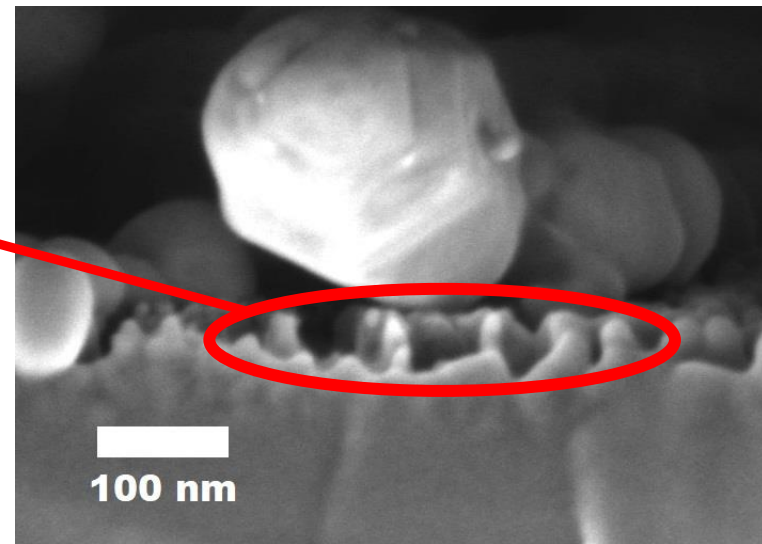
Silver-assisted Chemical Etching (SaCE)

Mechanism

10 s



Silicon
flakes

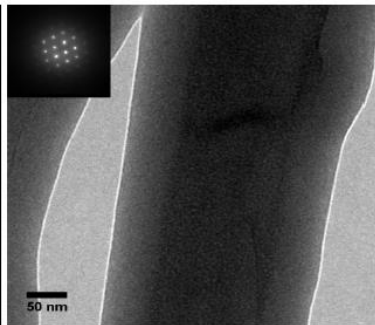
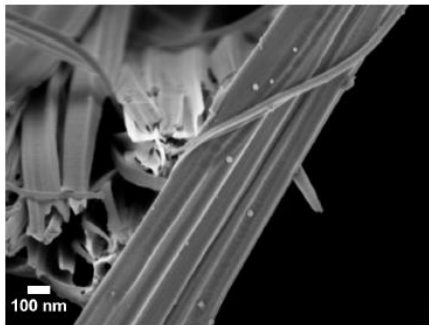


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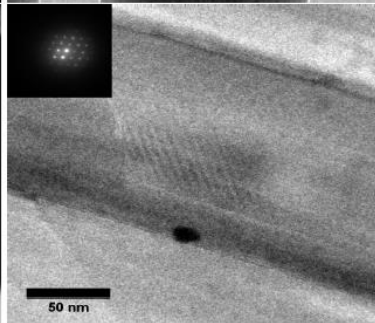
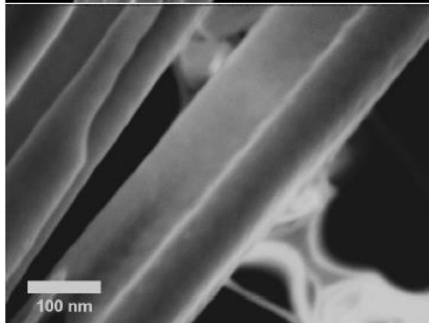
Silver-assisted Chemical Etching (SaCE)

20°C

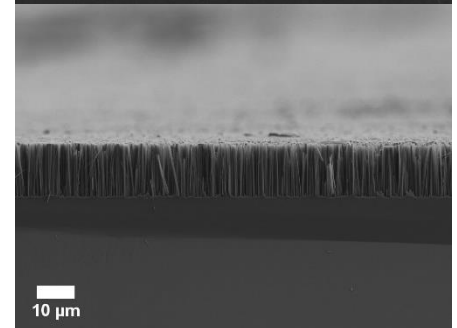
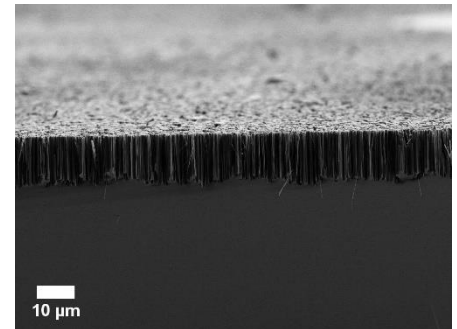
NWs Morphology



N-type (P)
Dopant Concentration $\sim 10^{15} \text{ cm}^{-3}$



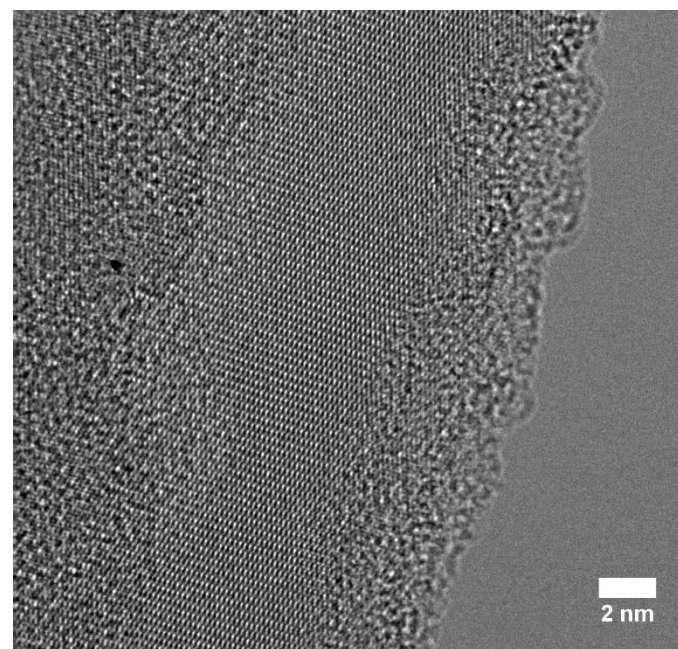
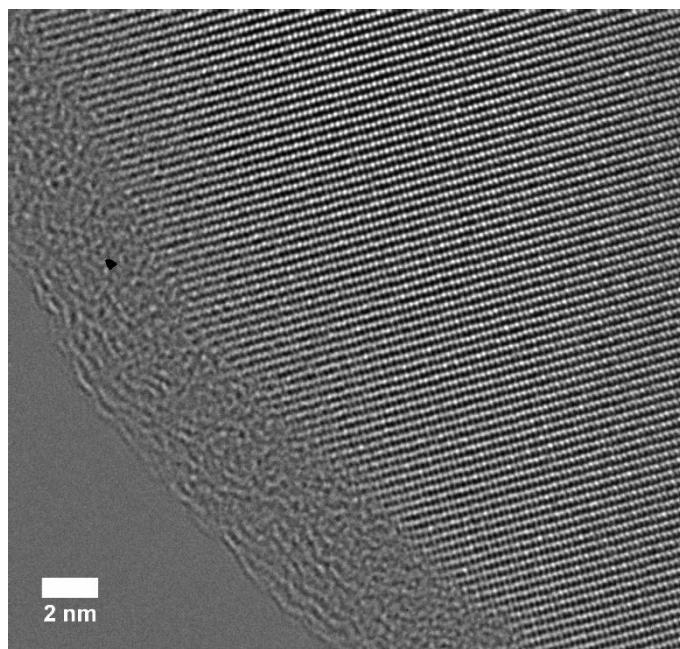
P-type (B)
Dopant Concentration $\sim 10^{15} \text{ cm}^{-3}$



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Silver-assisted Chemical Etching (SaCE)

NWs Morphology

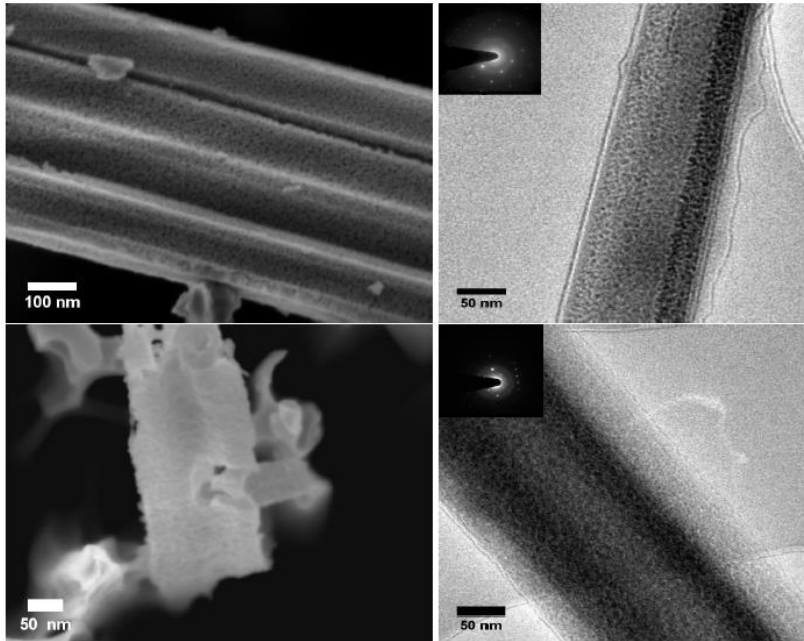


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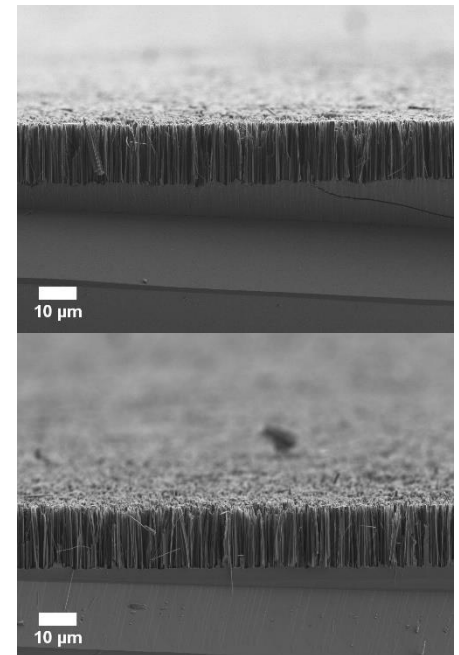
20°C

NWs Morphology



N+-type (P)
Dopant Concentration $\sim 10^{17} \text{ cm}^{-3}$

P+-type (B)
Dopant Concentration $\sim 10^{17} \text{ cm}^{-3}$



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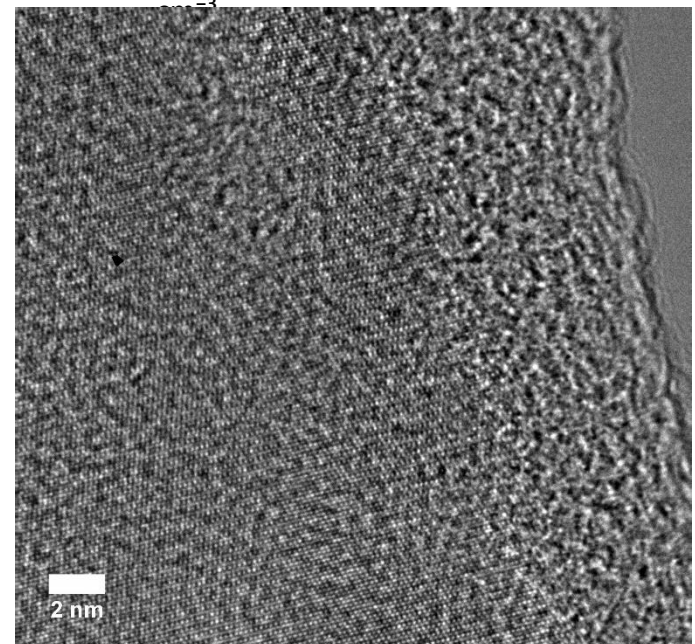
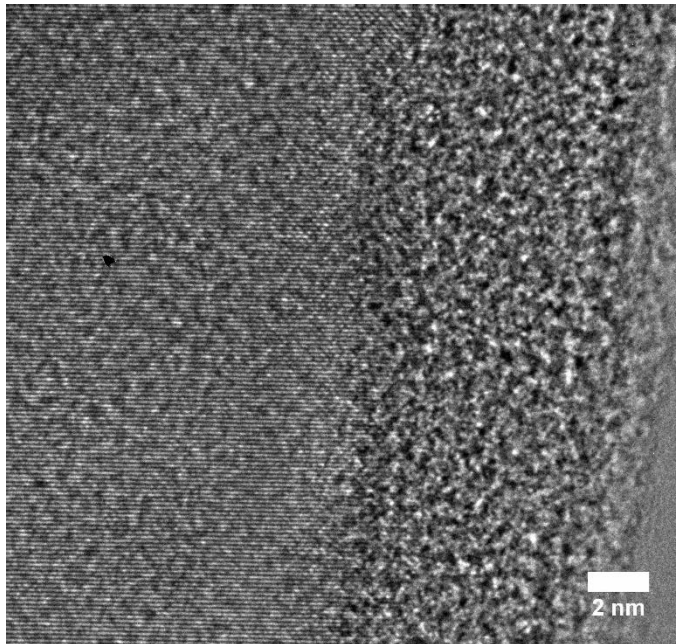
N+-type (P)

Dopant Concentration $\sim 10^{17} \text{ cm}^{-3}$

NWs Morphology

P+-type (B)

Dopant Concentration $\sim 10^{17}$

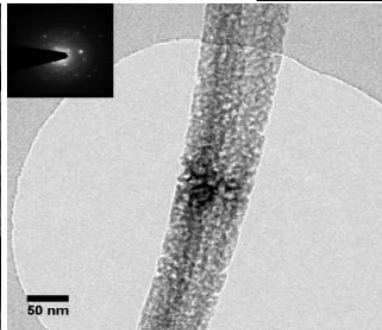
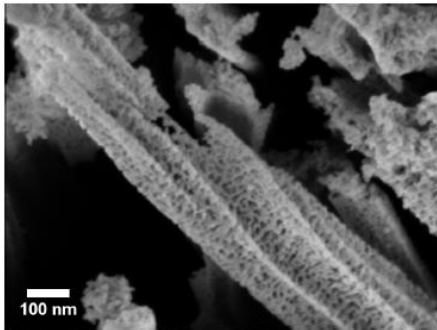


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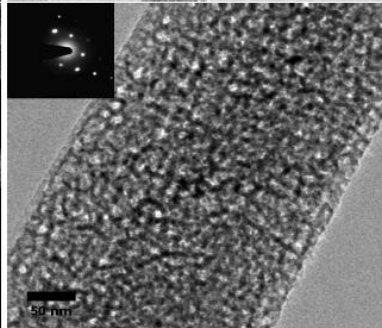
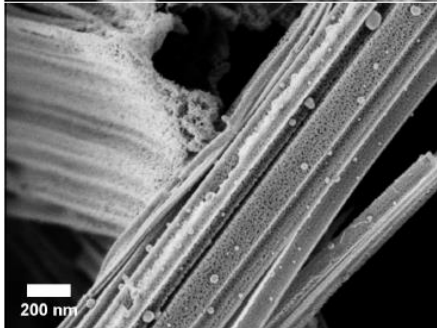
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20°C

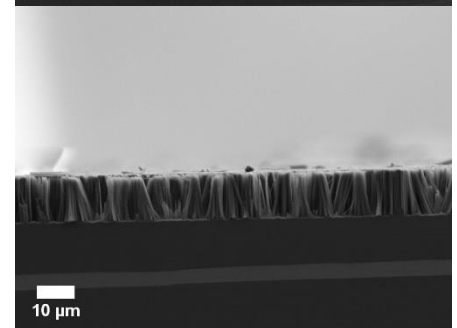
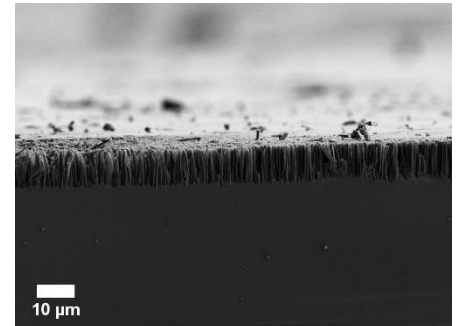
NWs Morphology



N++-type (P)
Dopant Concentration $\sim 10^{19} \text{ cm}^{-3}$

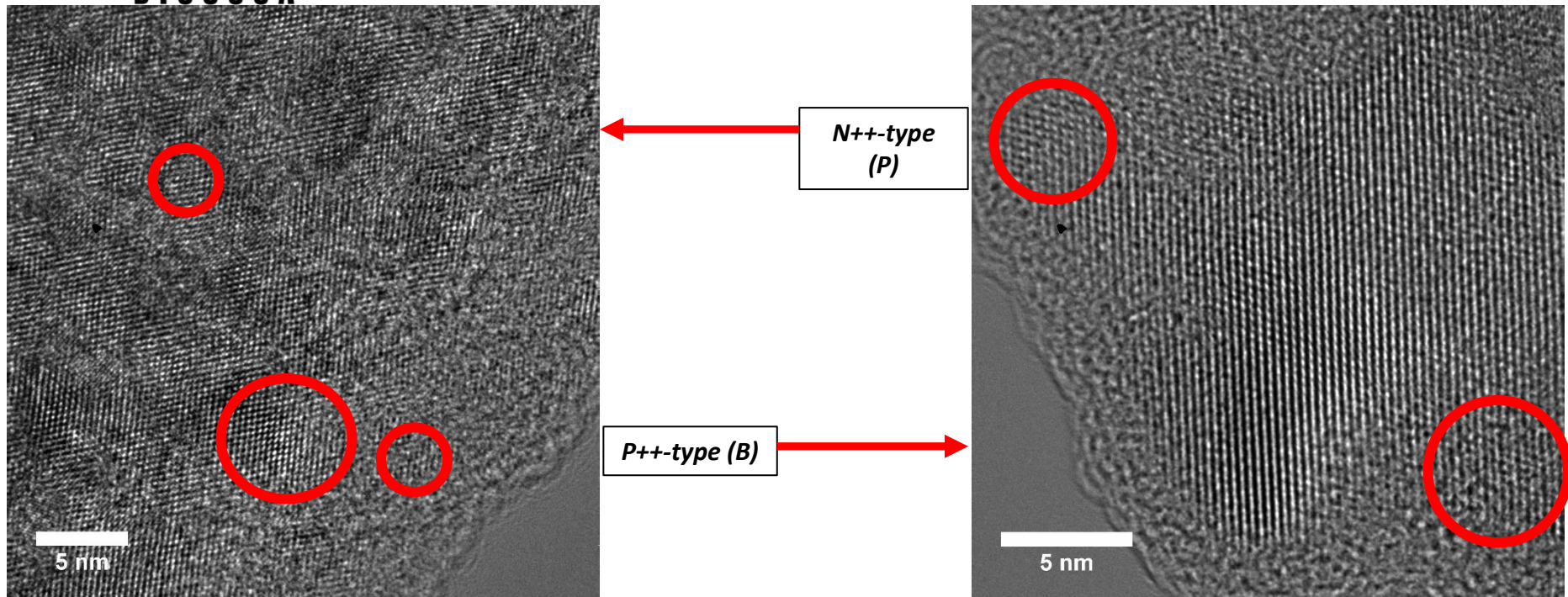


P++-type (B)
Dopant Concentration $\sim 10^{19} \text{ cm}^{-3}$



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Silver-assisted Chemical Etching (SaCE)



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